

# Introduction to surface plasmon coupled fluorescence

*L. Dolgov*

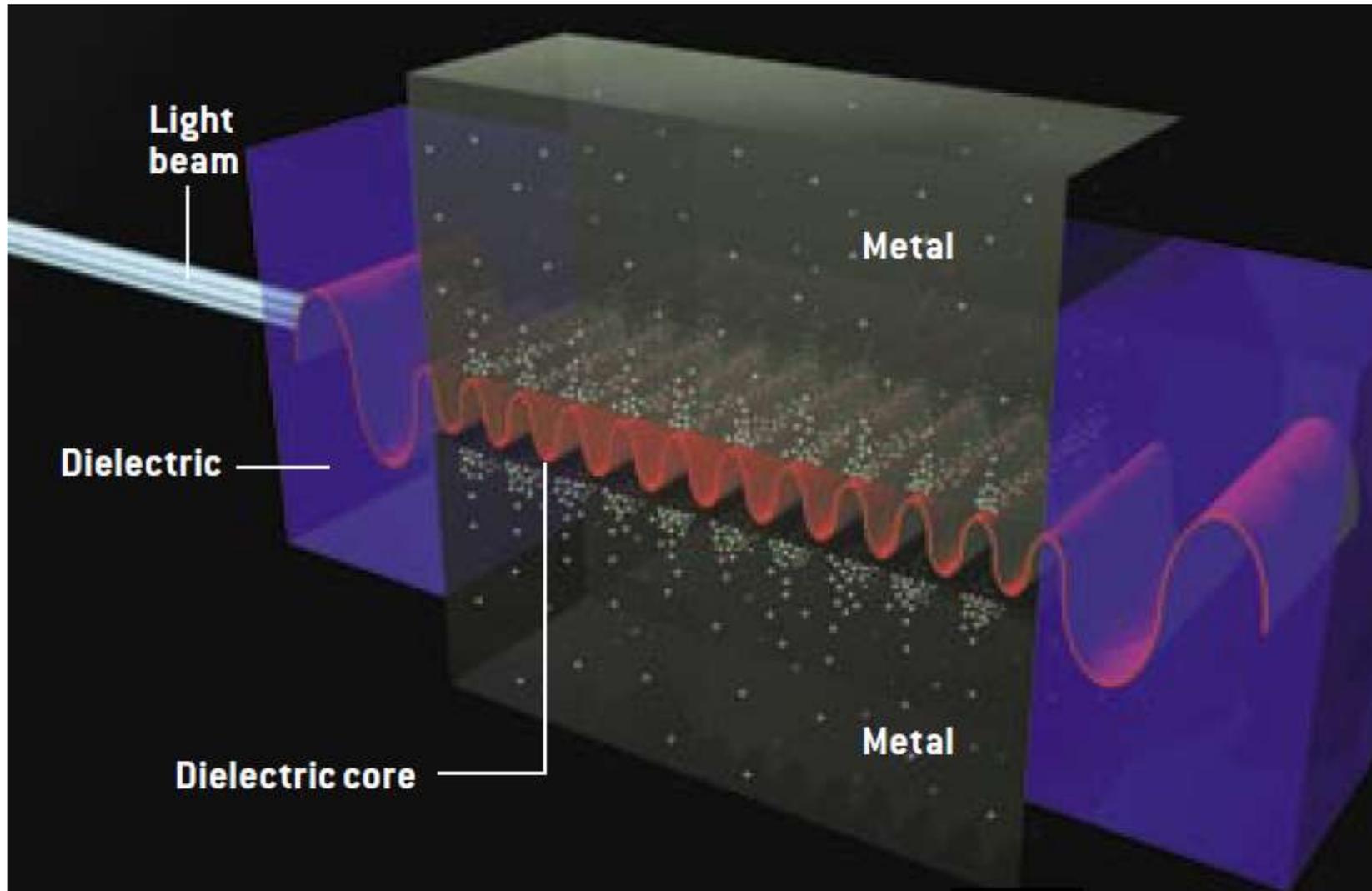
*Institute of Physics, University of Tartu, Laboratory of laser spectroscopy*

# Plan

1. Introduction: particular plasmonic effects and their applications.
2. How to excite surface plasmon waves? Nature of surface plasmon resonance.
3. Excitation of plasmons by prism coupling scheme.
4. Modification of prism coupling scheme for the fluorescent materials.
5. Some knowledge about localized plasmons and different ways for excitation of plasmons.

1. Introduction: particular plasmonic effects and their applications.

# Metal-dielectric structure: plasmon slot waveguide



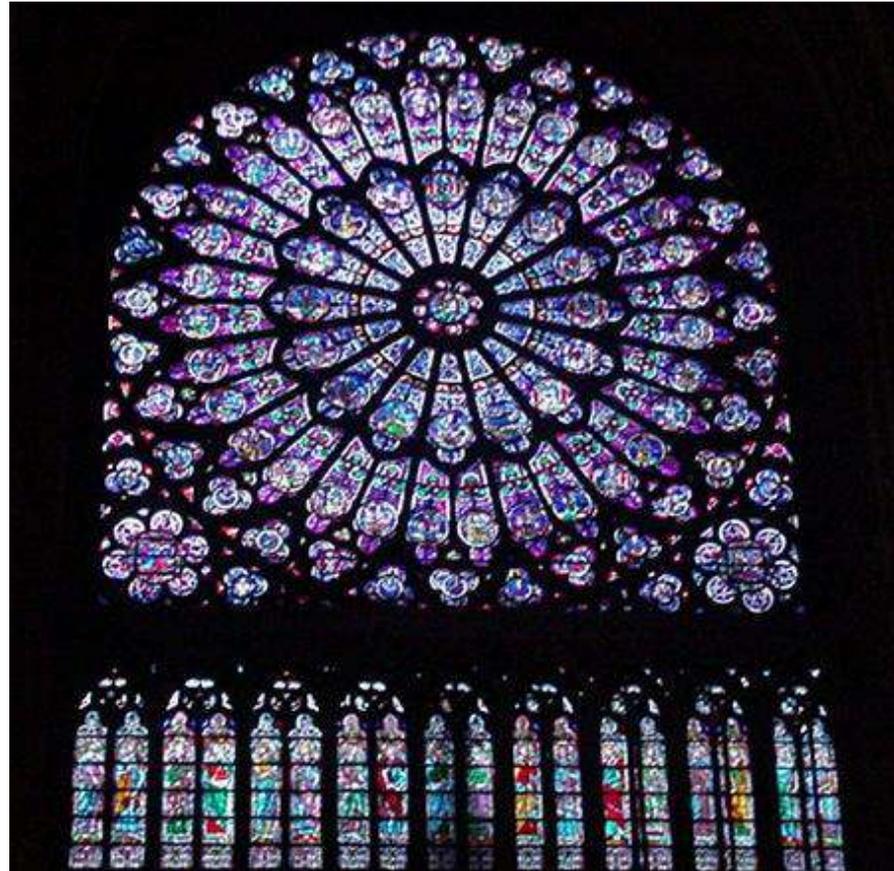
Atwater H.A. / Scientific American (2007).

# Ancient roots of plasmonics: Coloration effects caused by metal nanoparticles incorporated inside the glass



Lycurgus cup, 4thC AD, Rome

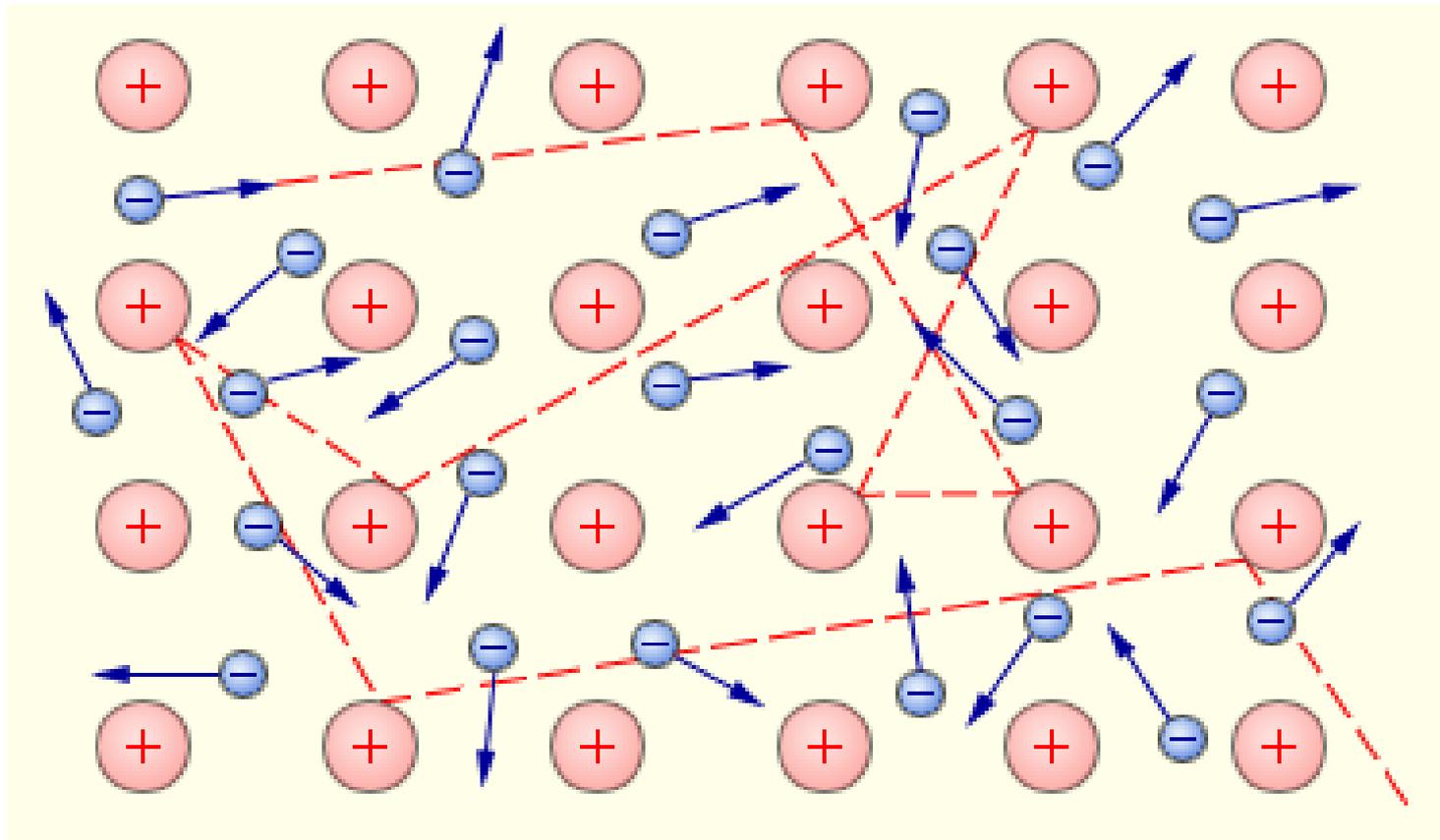
Atwater H.A. / Scientific American (2007).



1268 CE, Notre Dame de Paris

Lakowicz J. R. Plasmon-Controlled Fluorescence. A New Paradigm in Fluorescence Spectroscopy

# Classical representation of electrons in the metal



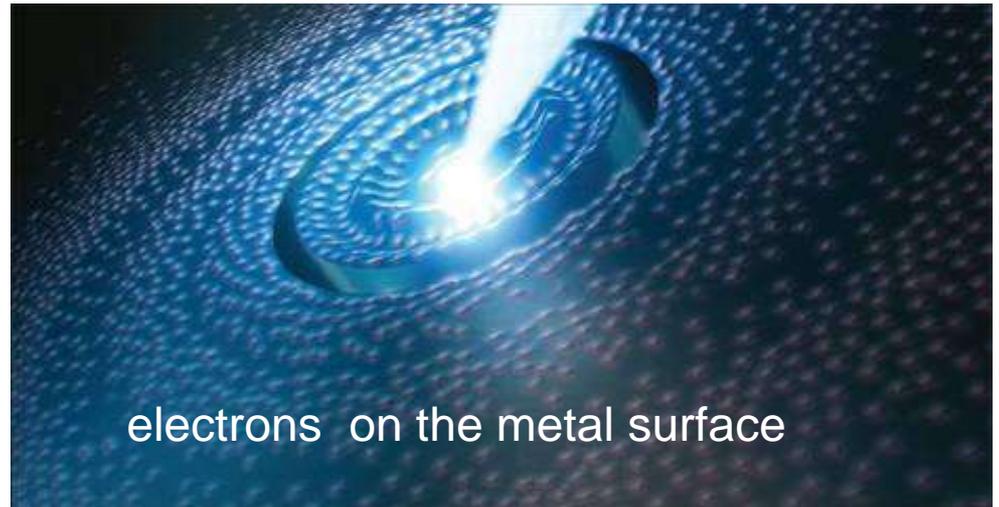
# Imagine plasmons

Surface waves on the water



<http://palscience.com>

Scheme of electronic density waves in the circular metal groove

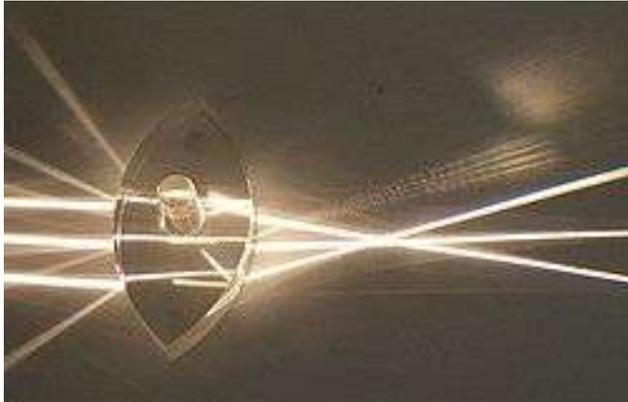


electrons on the metal surface

Atwater H.A. / Scientific American (2007).

Plasmons are the waves of electronic density on the metal surface

## Lens



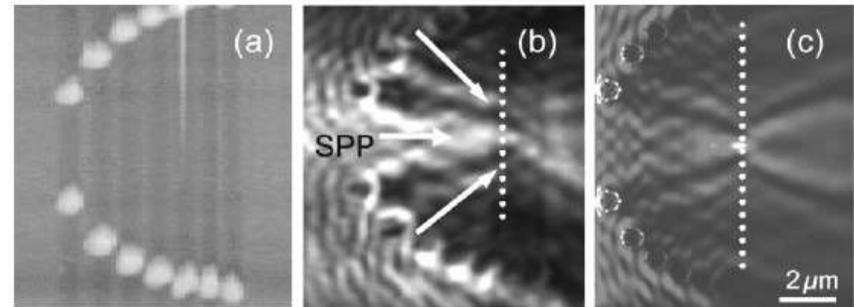
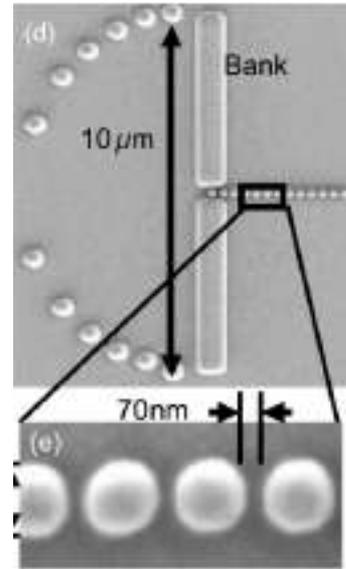
from wikipedia

## Optical waveguide



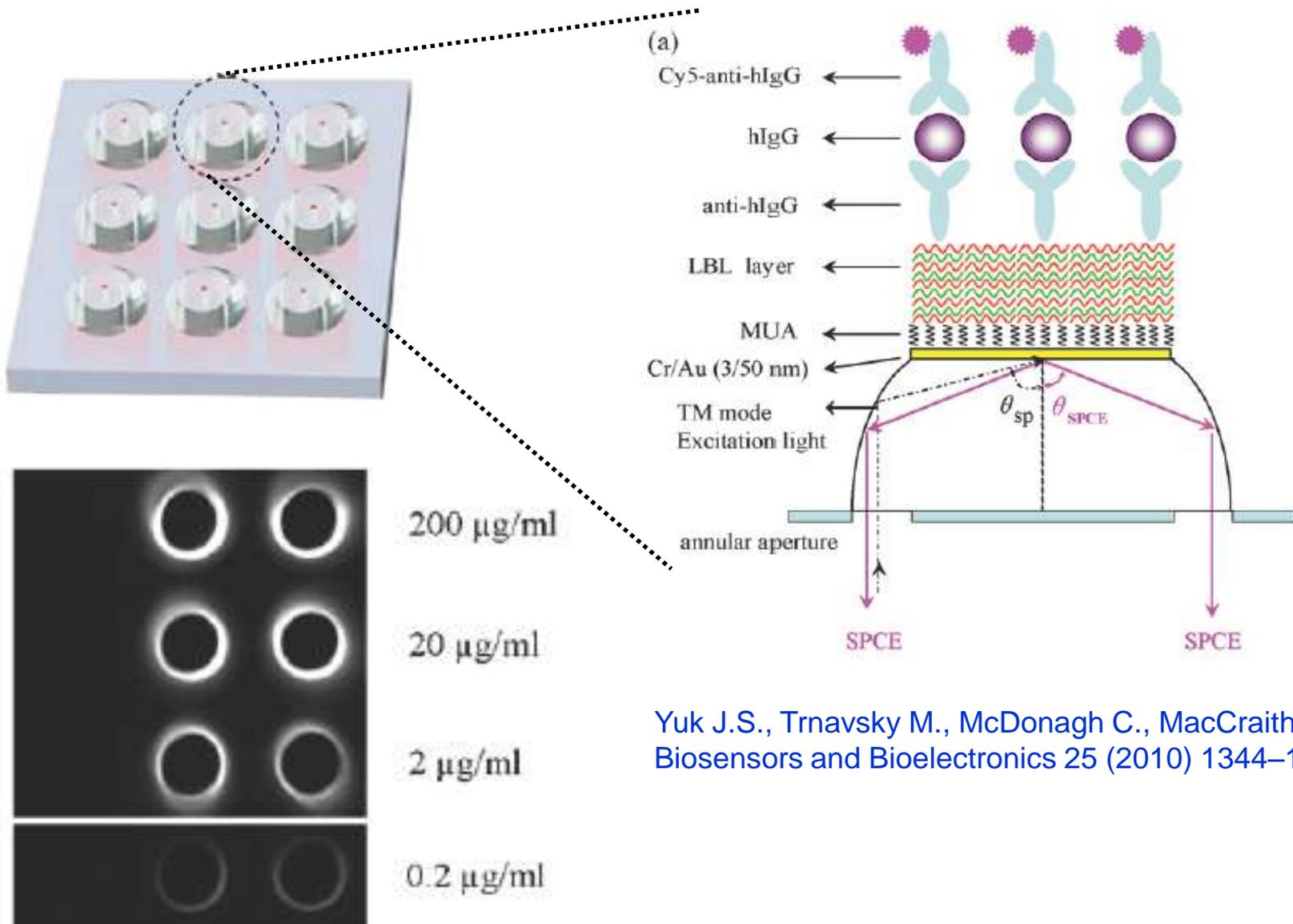
A TOSLINK fiber optic audio cable being illuminated at one end

## Plasmonic analog of condenser with waveguide



W. Nomura, M. Ohtsu, T. Yatsui, Appl. Phys. Lett. 86, 181108 (2005).

# Plasmons for sensitive optical detectors

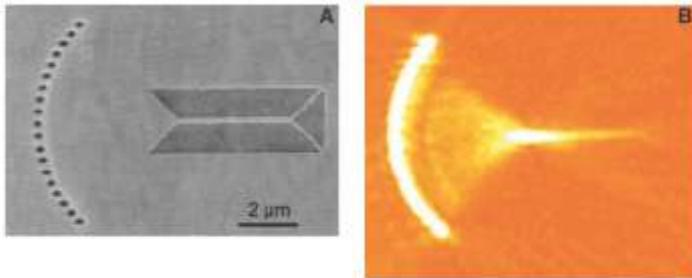


Yuk J.S., Trnavsky M., McDonagh C., MacCraith B. // Biosensors and Bioelectronics 25 (2010) 1344–1349.

# Application of plasmons localized in nanoparticles

Enhanced electrical field of light near the nanoparticles

Focusing energy and its transfer to the subwavelength waveguides



W. Nomura, M. Ohtsu, T. Yatsui, Appl. Phys. Lett. 86, 181108 (2005).

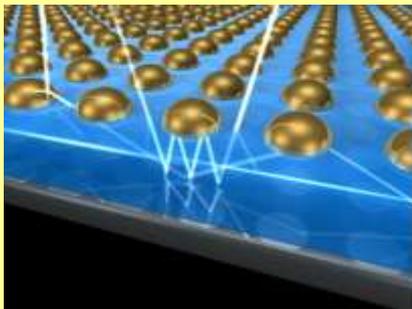
Enhanced absorption of light

Transformation of absorbed light into electricity

Nonradiative transfer of absorbed light to the fluorophore

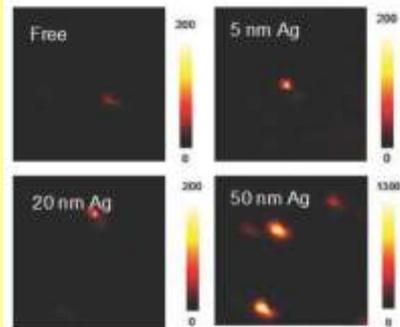
Transfer of absorbed light to heat

Plasmonic solar cells with higher efficiency



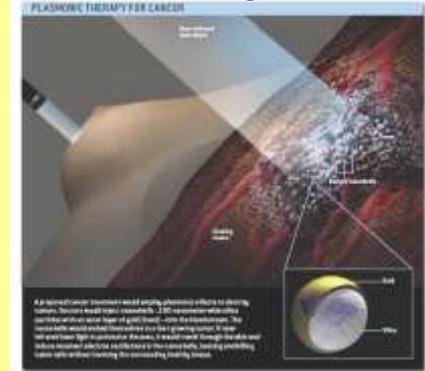
[www.erbium.nl/research.html](http://www.erbium.nl/research.html)

Improved fluorescent materials



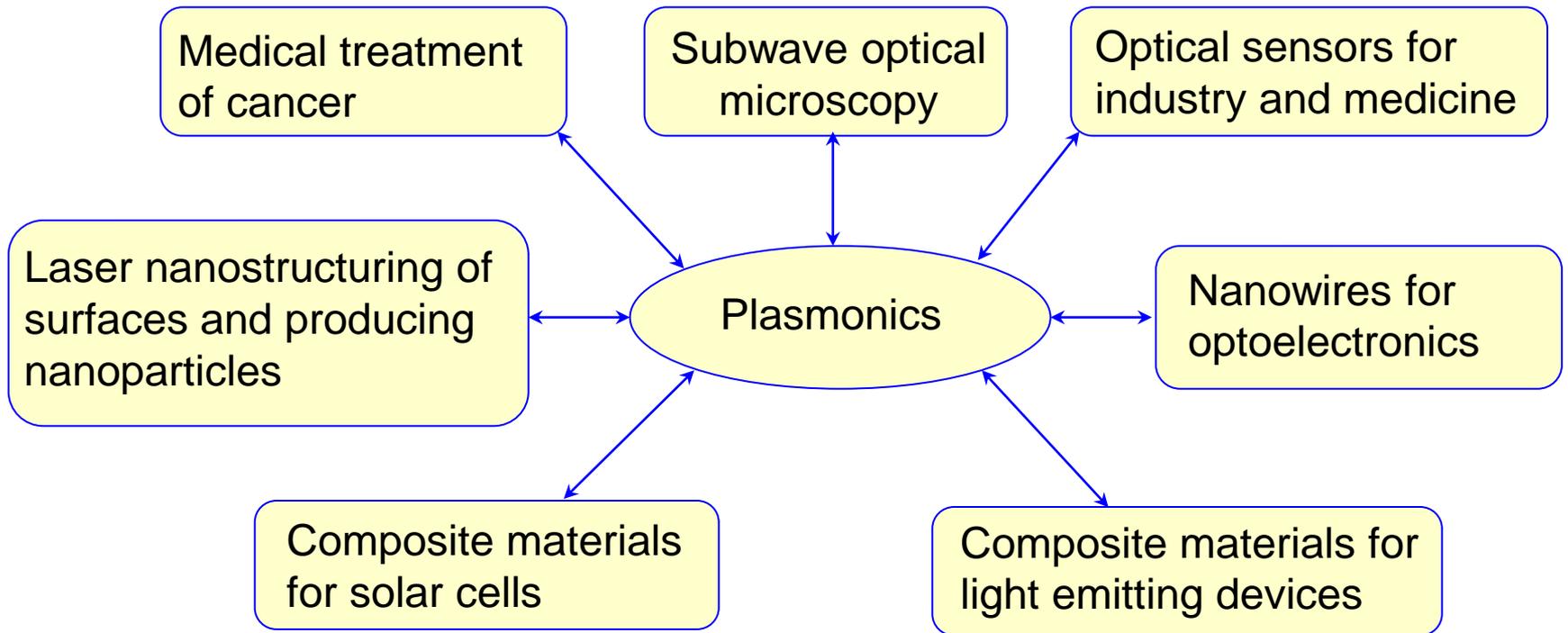
Lakowicz J. R. Plasmon-Controlled Fluorescence. A New Paradigm in Fluorescence Spectroscopy

Thermal curing of cancer



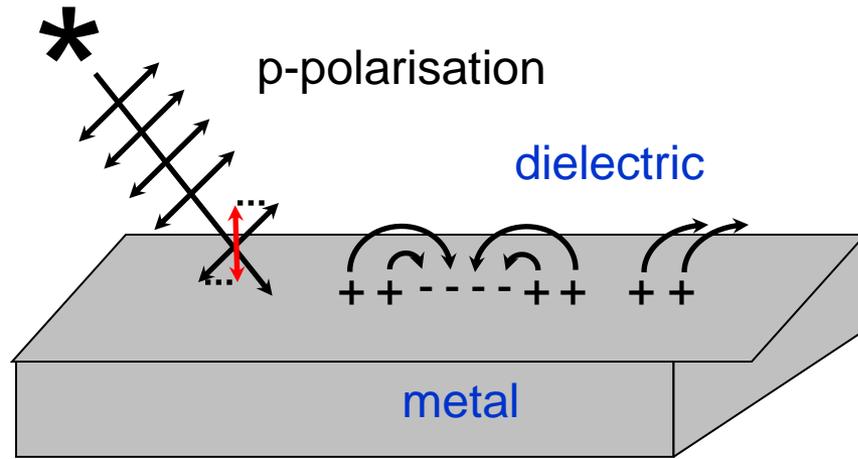
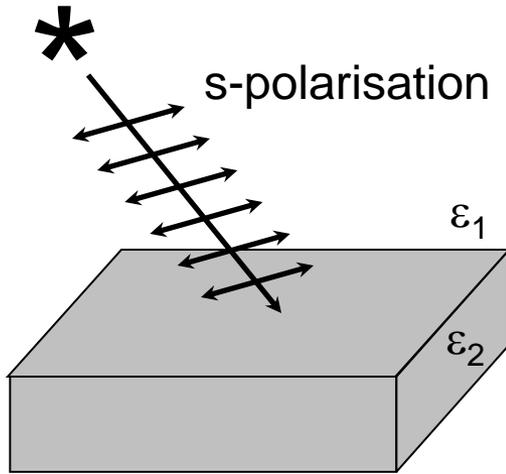
Atwater H.A. / Scientific American (2007).

# Plasmons for...

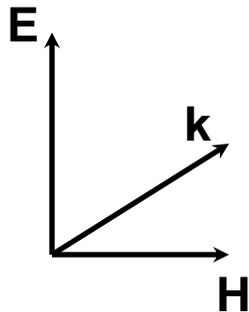


2. How to excite surface plasmon waves ?  
Nature of surface plasmon resonance.

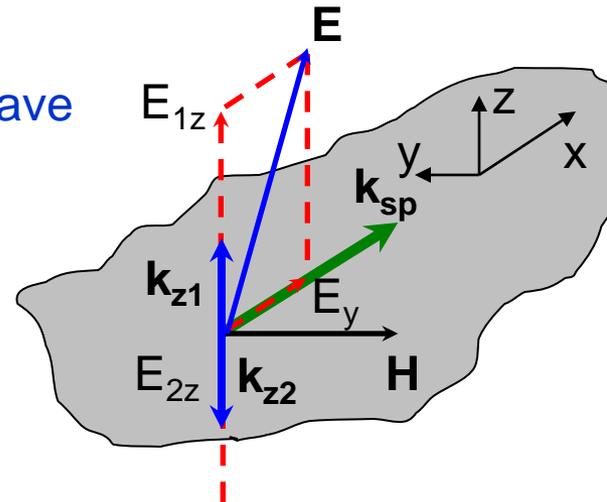
# Surface plasmon waves are partially longitudinal



usual wave



surface wave



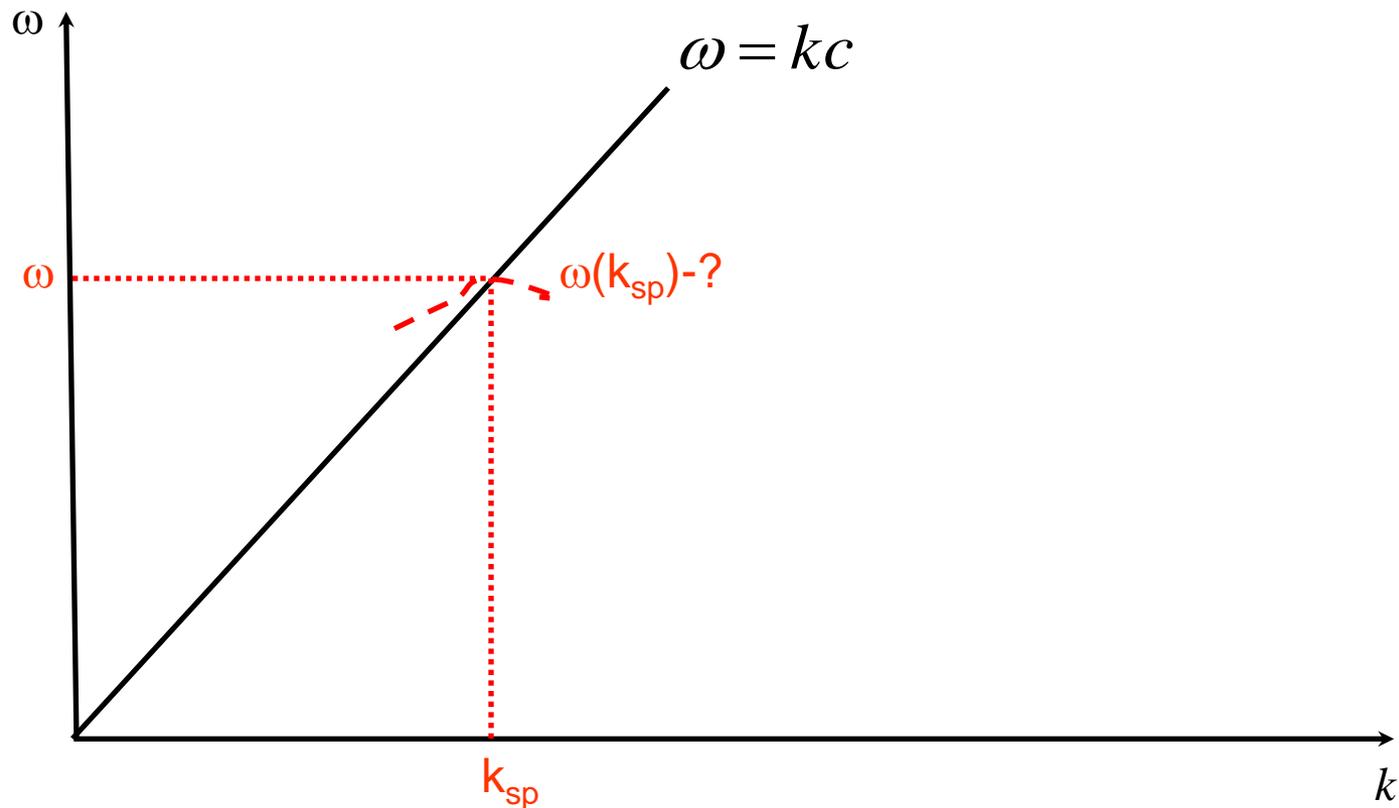
$\mathbf{k}$  – wave vector,  
 $\mathbf{E}$  – electric field strength,  
 $\mathbf{H}$  – magnetic strength

$$\mathbf{E} = \mathbf{E}_0 e^{\mp k_{z1,2} z} e^{ik_{sp} x - i\omega t}$$

# Dispersion relation for the wave vectors

$k=k_{sp}$  – surface plasmon resonance conditions

Light wave



# Definition of wave vector for surface plasmon

$$E = E_0 e^{\mp k_{z1,2} z} e^{ik_{sp} x - i\omega t}$$

- electric field of surface wave

$$H = H_0 e^{\mp k_{z1,2} z} e^{ik_{sp} x - i\omega t}$$

- magnetic field of surface wave

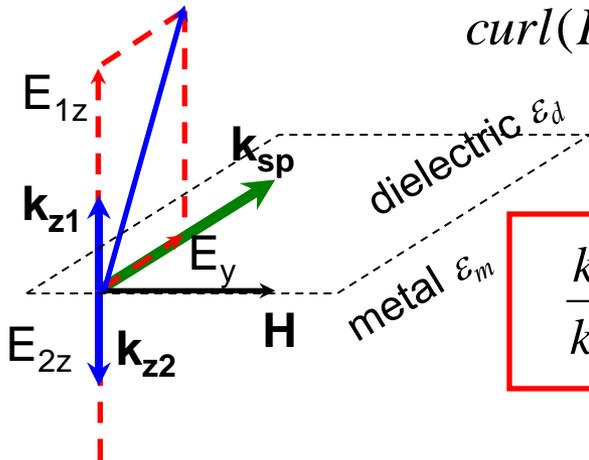
$$k_{z1}^2 + k_{sp}^2 = \epsilon_d k^2$$

$$k_{z2}^2 + k_{sp}^2 = \epsilon_m k^2$$

- connection between the components of the wave vectors

$$\text{curl}(\vec{H}) = \frac{1}{c} \frac{\partial \vec{E}}{\partial t}$$

- Maxwell's equation for magnetic field



$\epsilon_d$  - real part of permittivity for dielectric

$\epsilon_m$  - real part of permittivity for metal

$$\frac{k_{z1}}{k_{z2}} = \frac{\epsilon_d}{\epsilon_m}$$

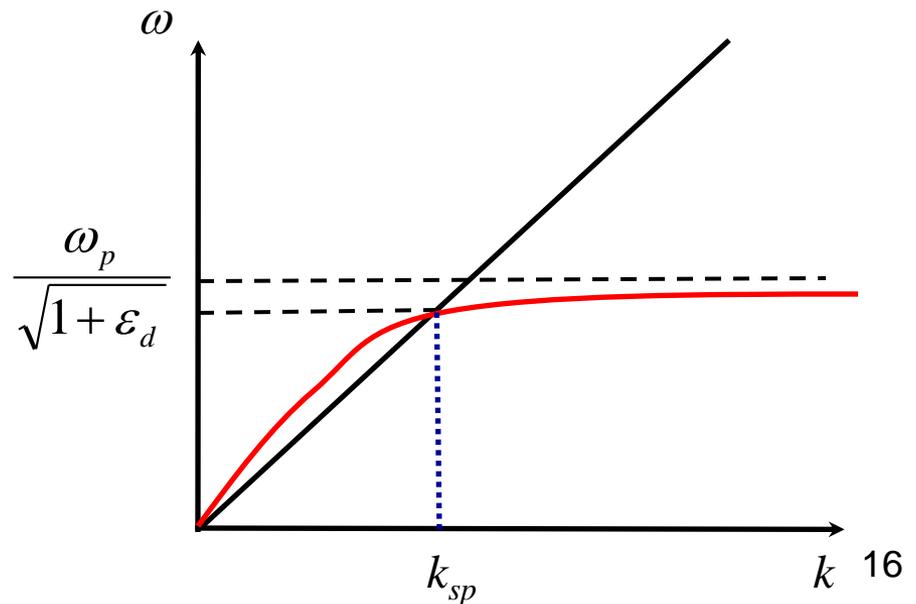
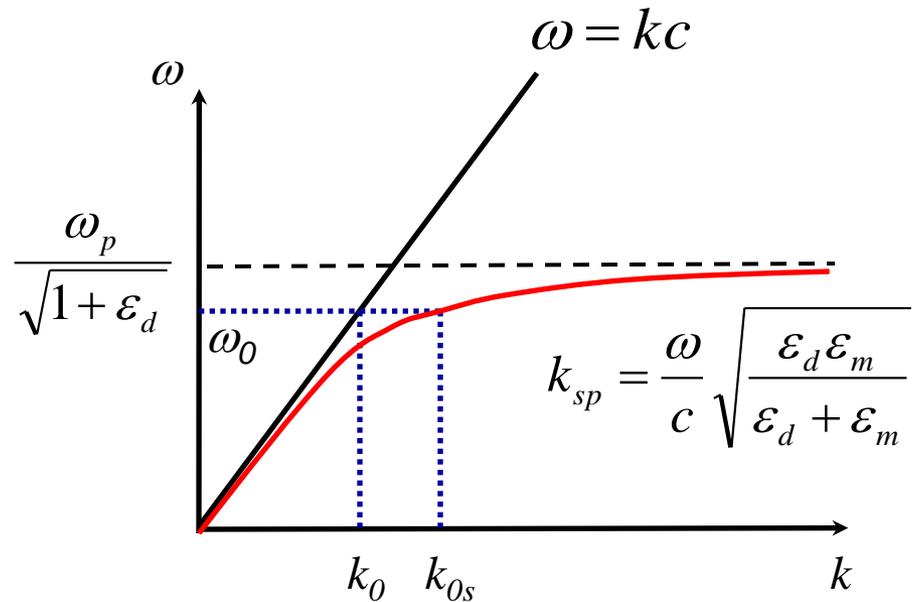
$$k_{sp} = k \sqrt{\frac{\epsilon_d \epsilon_m}{\epsilon_d + \epsilon_m}}$$

- wave vector of surface plasmon

Wave vector of light  $k_0$  passing through the medium at fixed frequency  $\omega_0$  is smaller than wave vector of surface plasmon  $k_{0s}$ :

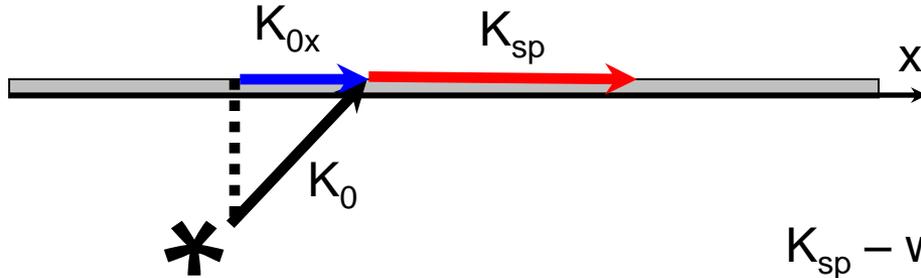
$$\omega_p = \frac{Ne^2}{m_e \epsilon_0} \quad \text{- volume plasmon frequency}$$

It is needed to increase the wave vector of light up to the wave vector of plasmon  $k_{sp}$ :



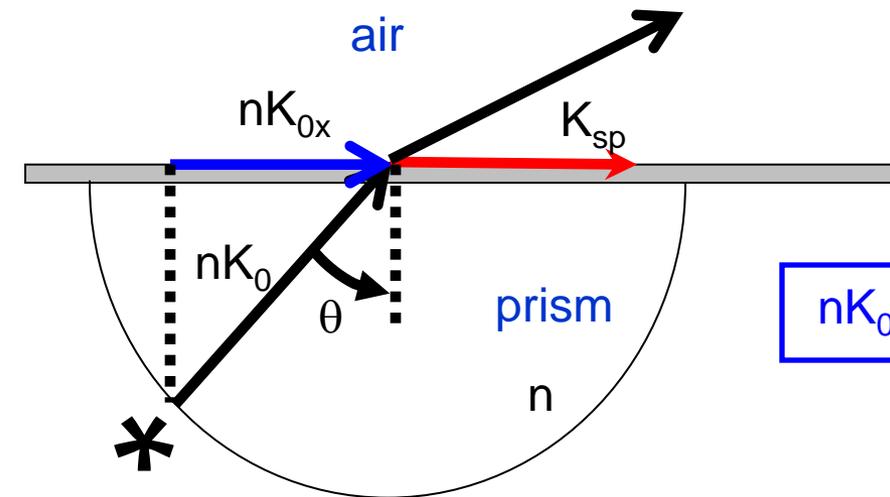
### 3. Excitation of plasmons by prism coupling scheme

# Hemispherical prism for increase wave vector of light



$K_0 = \omega/v$  – wave vector of incident light  
 $K_{0x}$  – projection of wave vector on the surface

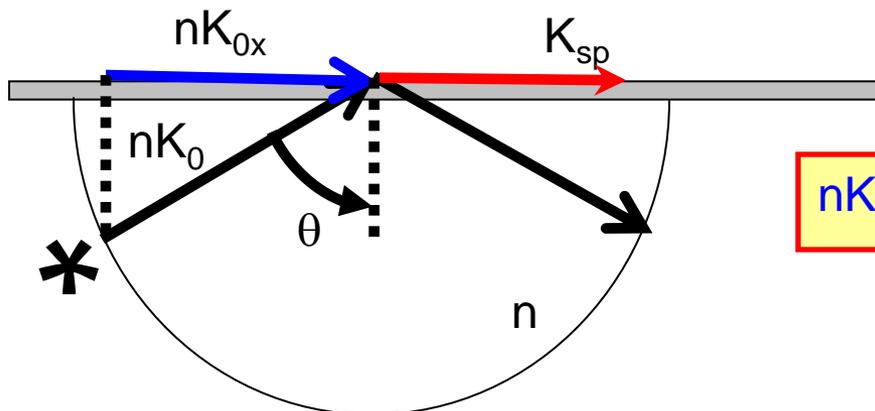
$K_{sp}$  – wave vector of the surface plasmon wave



$K_{0x} < K_{sp}$  - there is no surface wave

$$\sin \theta < 1/n$$

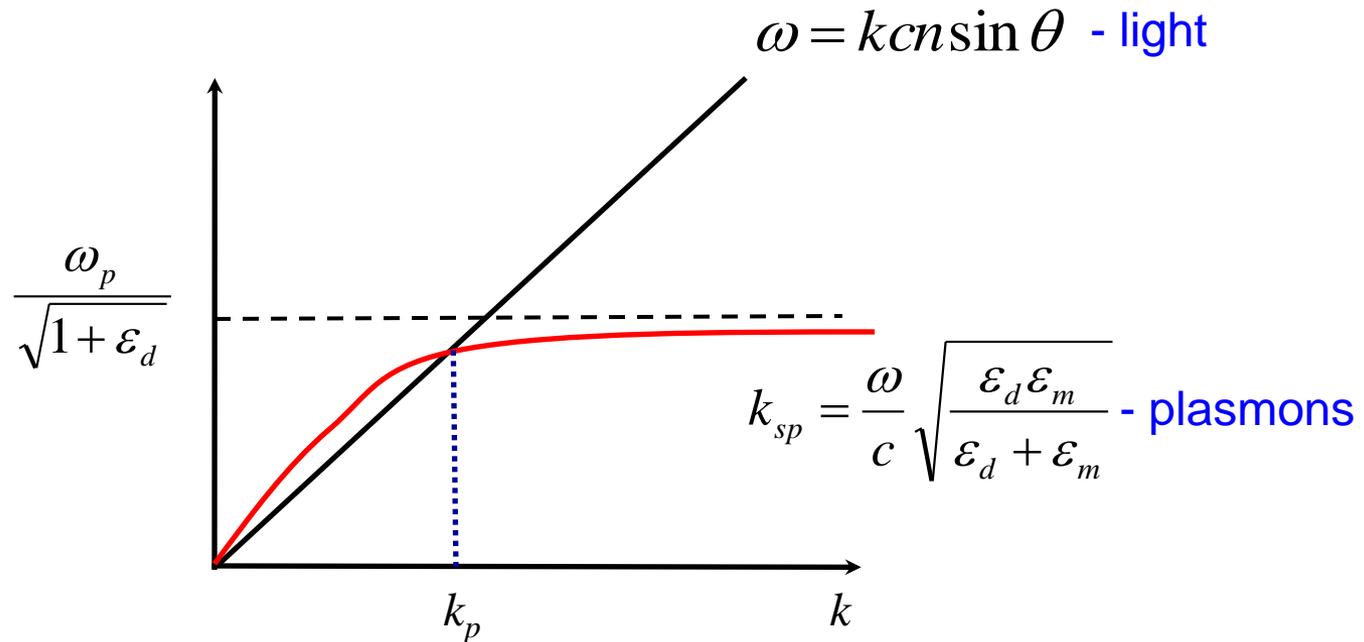
$nK_{0x} \sin \theta < K_{sp}$  - there is no surface wave still



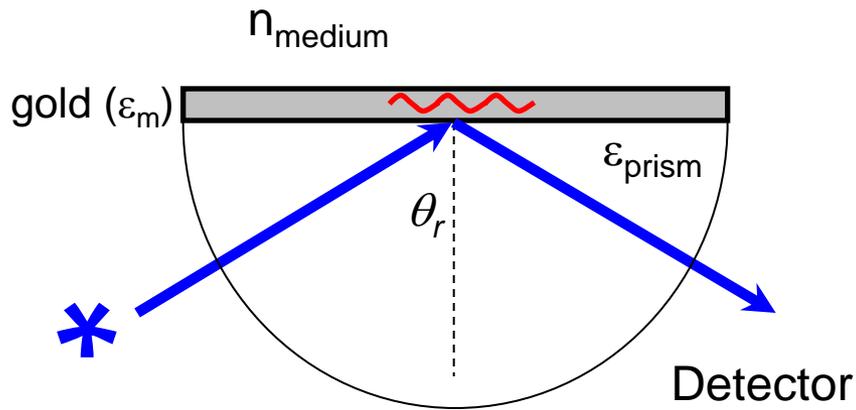
$$\sin \theta > 1/n$$

$nK_{0x} \sin \theta \sim K_{sp}$  - needed for surface wave

# Dispersion relation for the wave vectors in case of surface plasmon resonance

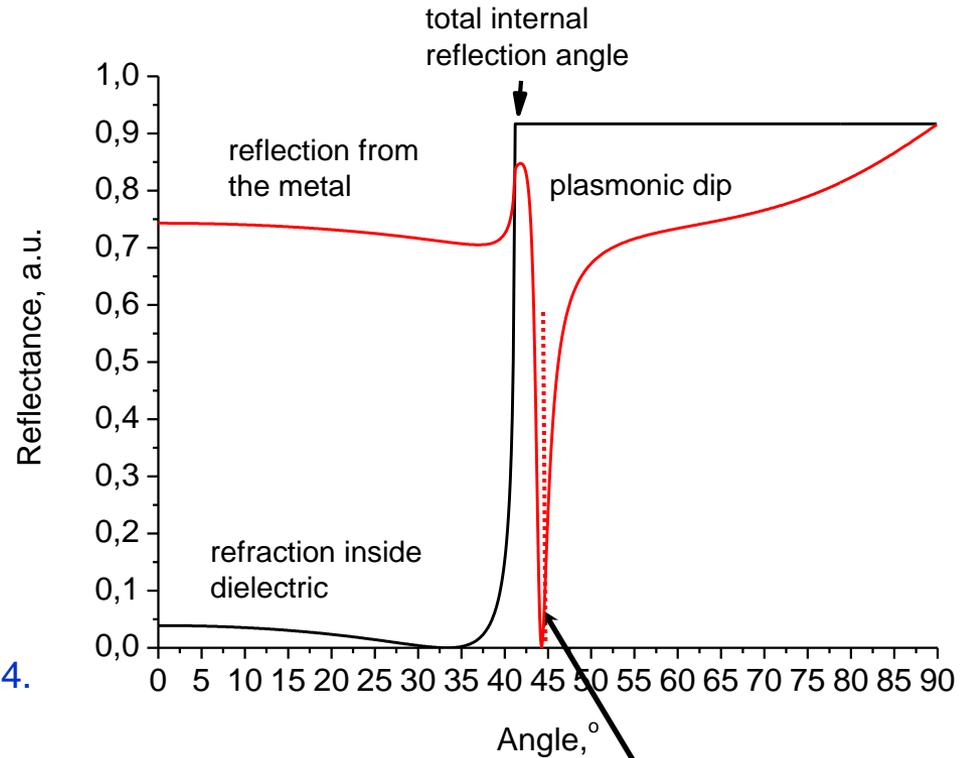


# Inducing of plasmons by Kretschmann scheme



## Kretschmann geometry of experiment

Kretschmann E. // Z. Physik, 1971, B. 241, S 313-324.



$$k_{prism} = k_{sp}$$

$$k n \sin \theta = k \sqrt{\frac{\epsilon_m \epsilon_{air}}{\epsilon_m + \epsilon_{air}}} + \Delta\beta$$

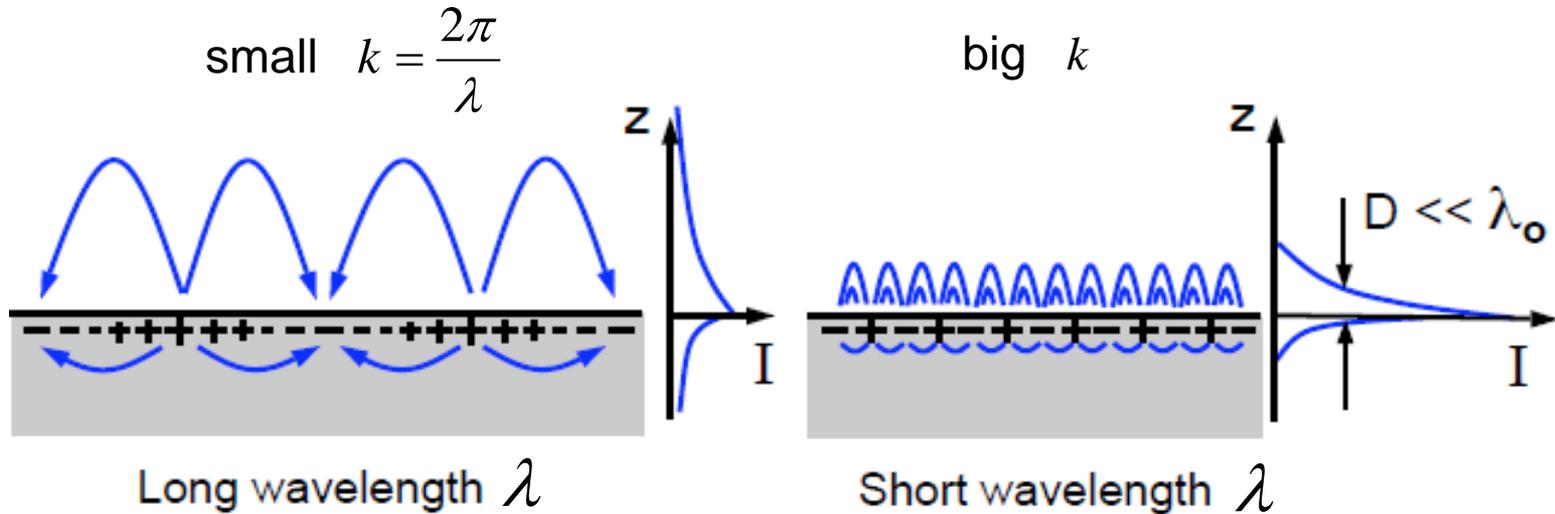
$$\theta = \theta_r$$

$$v = v_s$$

$$W_{reflected} = W_{incident} - W_{plasmon}$$

$\Delta\beta$  - parameter, which depends on the thickness of metal film

# Plasmons with big and small wave vector $k$

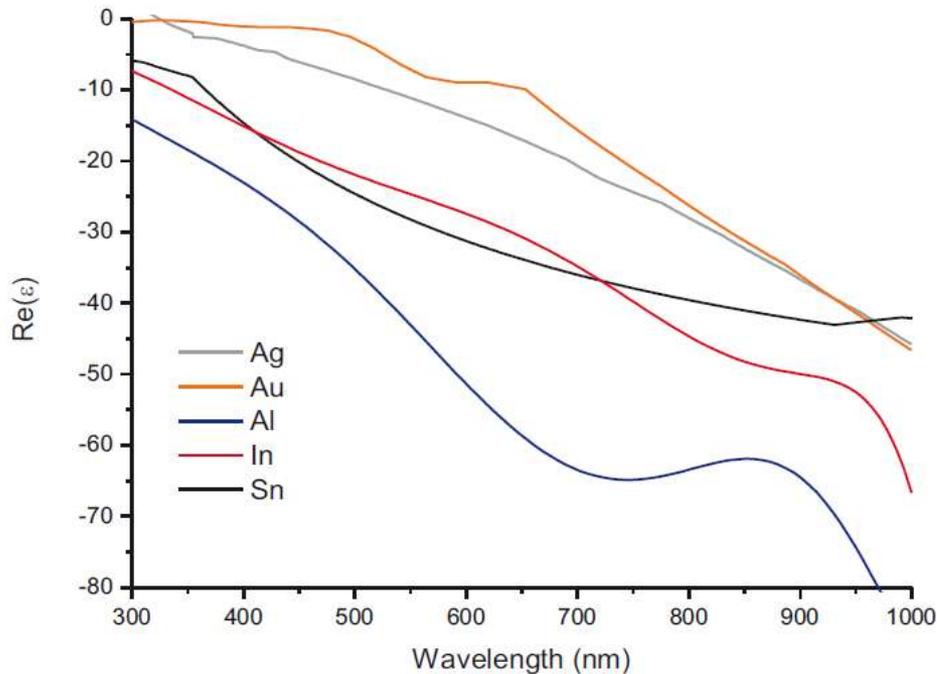


At big  $k$ :

$$\omega = \omega_{sp} \text{ when } : \epsilon_m = 1 - \frac{\omega_p^2}{\omega^2} = -\epsilon_d \rightarrow \omega^2 - \omega_p^2 = -\epsilon_d \omega^2 \rightarrow \omega^2 = \frac{\omega_p^2}{1 + \epsilon_d} \rightarrow \omega = \frac{\omega_p}{\sqrt{1 + \epsilon_d}}$$

$$n \sin \theta = \sqrt{\frac{\epsilon_d \epsilon_m}{\epsilon_d + \epsilon_m}}$$

# Real part of metal permittivity vs the wavelength of light

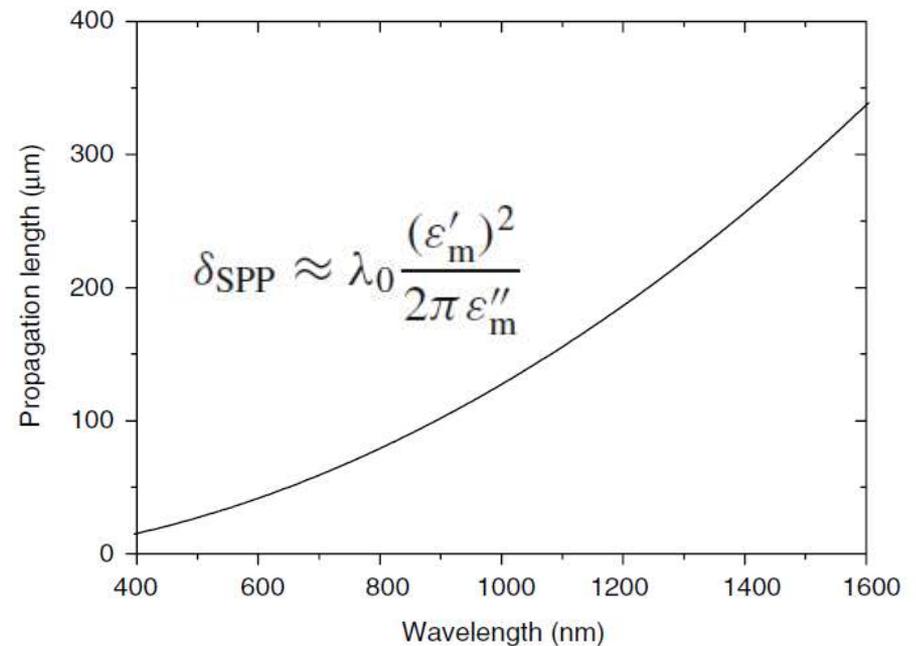
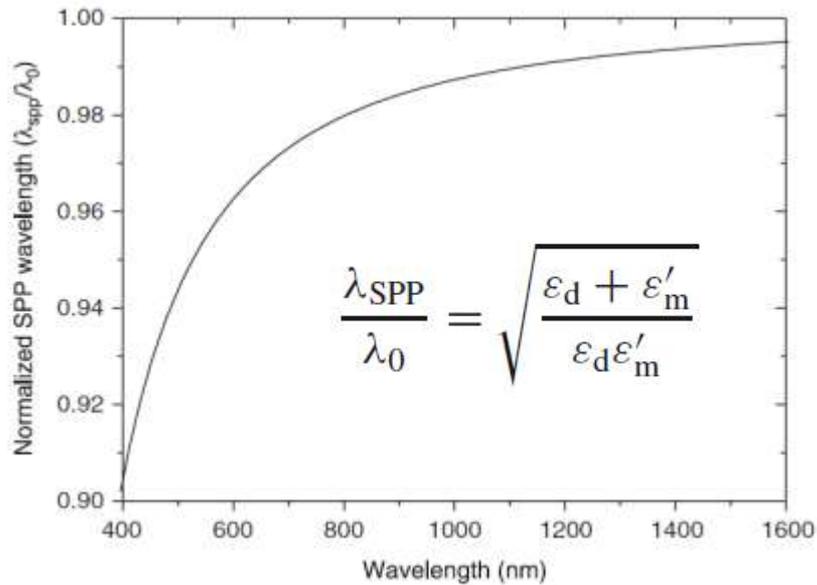


For metal-vacuum interface surface plasmon resonance must be at  $\epsilon_m = -1$

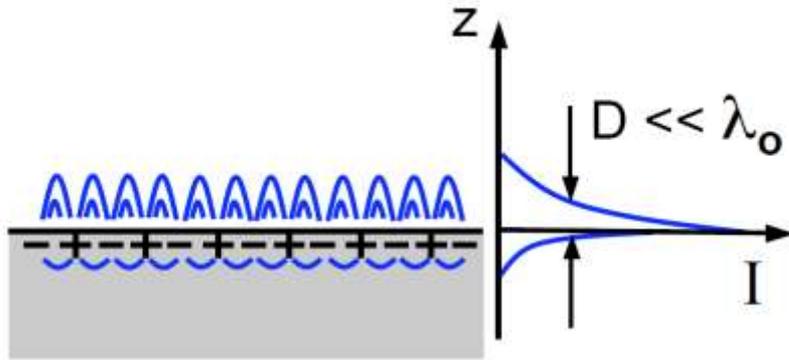
Oliver Benson Elements of Nanophotonics

Metal	Resonance wavelength of light, nm
Au	~520
Ag	~380
Al	<300

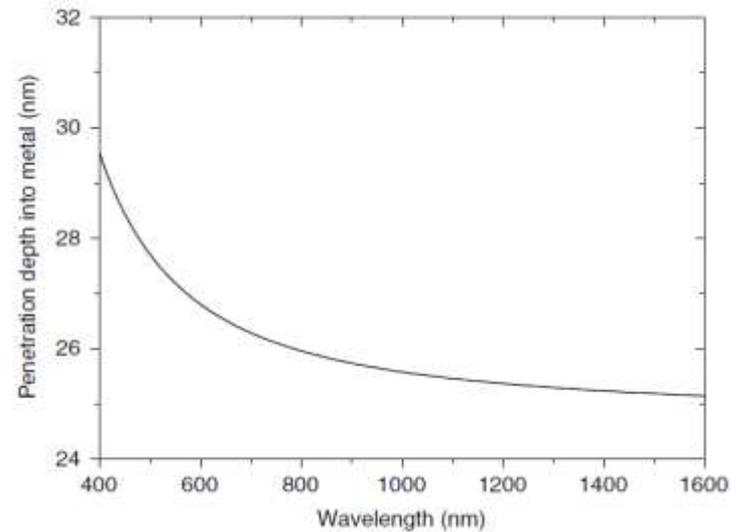
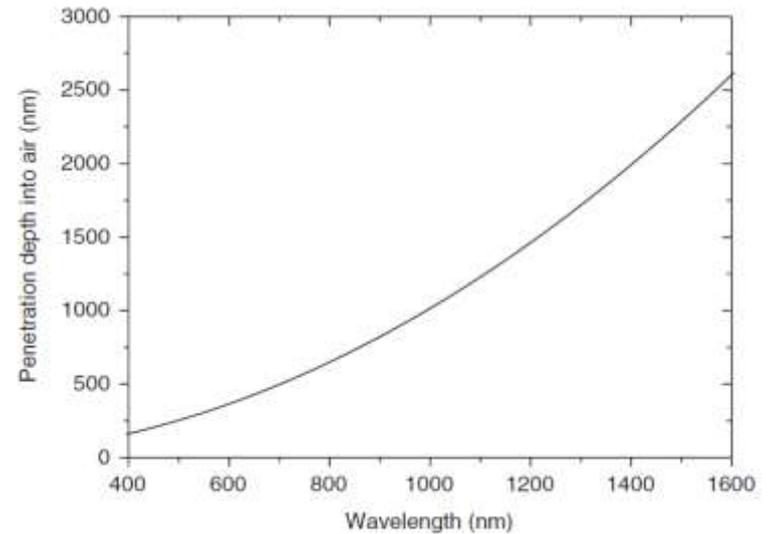
# Wavelengths and propagation lengths of surface plasmons



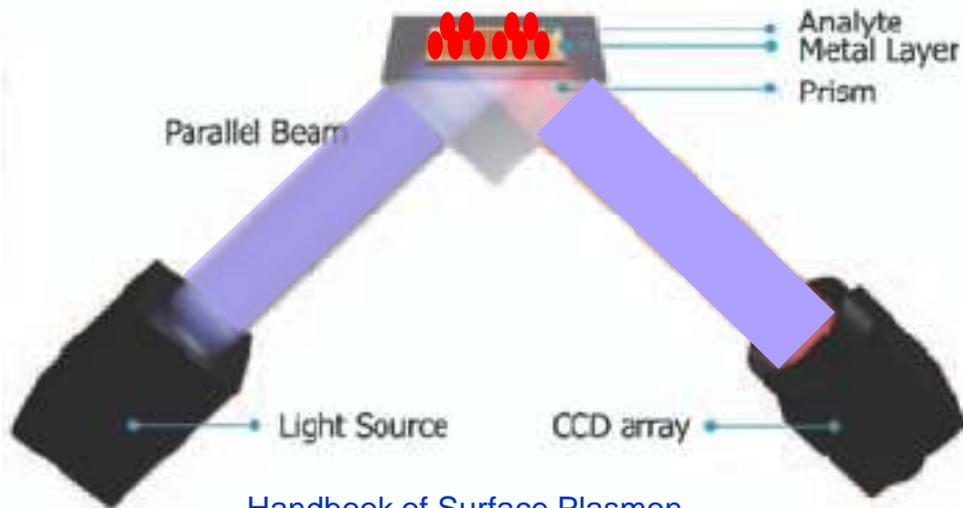
# Surface plasmon penetration depths



V. M. Shalaev Nanophotonics. Lectures

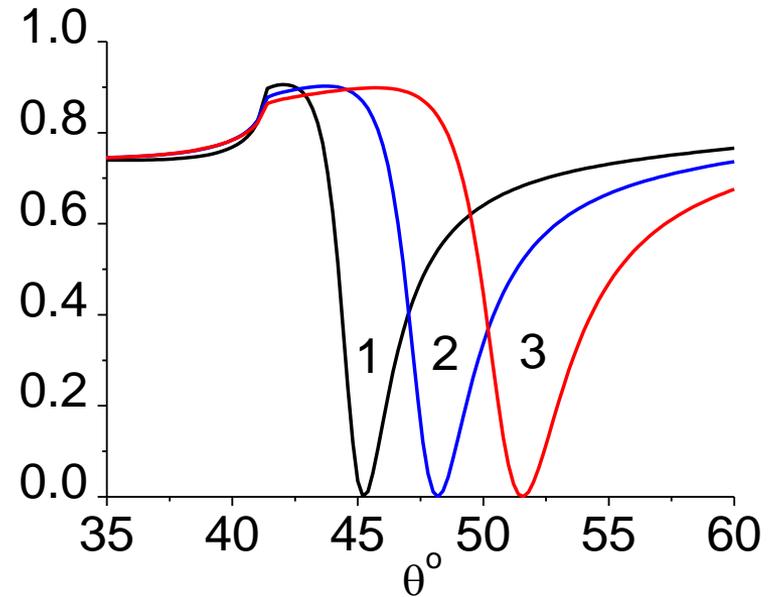


# Plasmonics for the optical sensing



Handbook of Surface Plasmon Resonance / Editors R.B.M. Schasfoort and A. J. Tudos

## Reflection



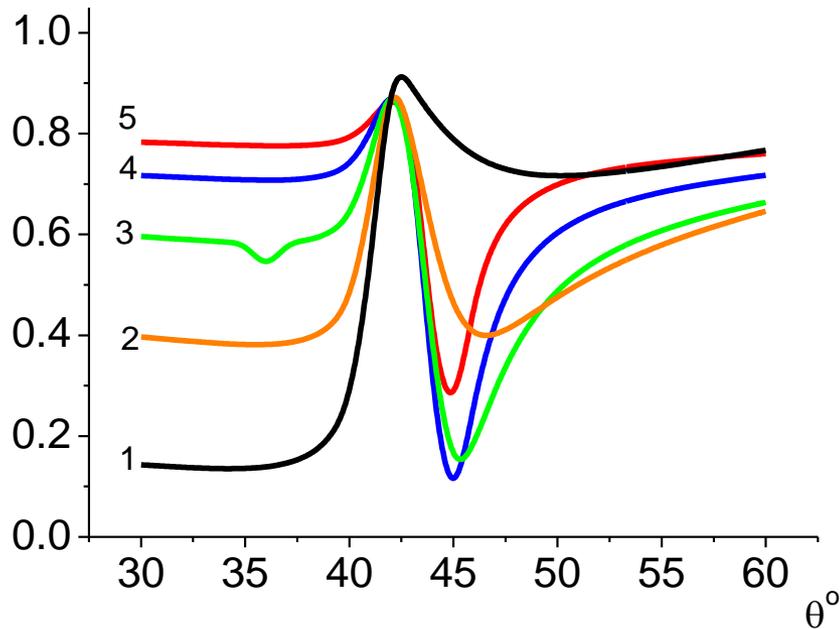
$n_{\text{analyte}}$	$\theta^\circ$
1	45.23°
1.01	45.8°
1.05	48.2°
1.07	49.4°
1.1	51.4°

Prism is metallized by gold film (50 nm)  
wavelength of incident light is 583 nm

- 1)  $n_{\text{analyte}}=1$ ,
- 2)  $n_{\text{analyte}}=1.05$ ,
- 3)  $n_{\text{analyte}}=1.1$ .

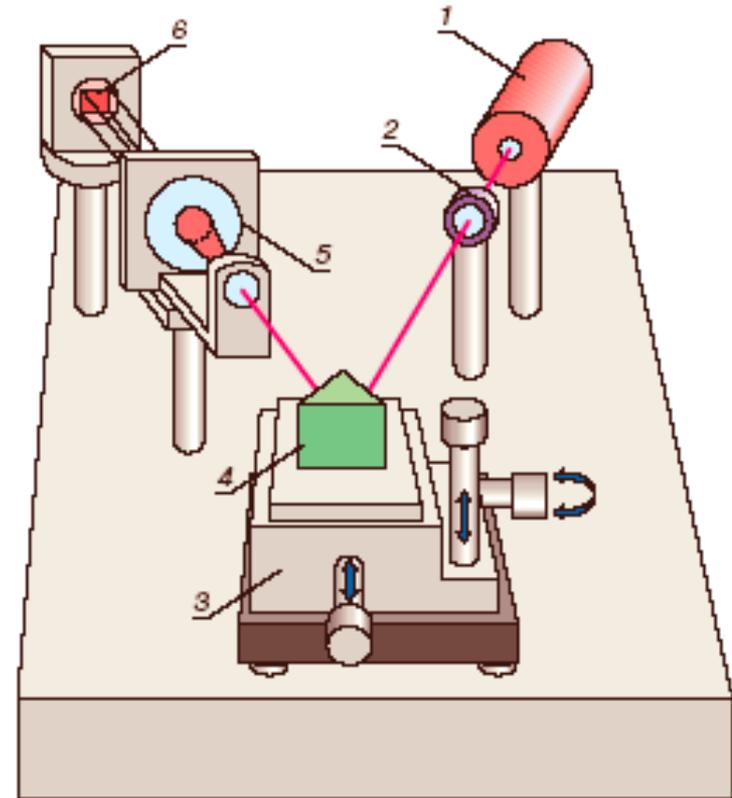
# Plasmonics for subwave microscopy

Reflectance

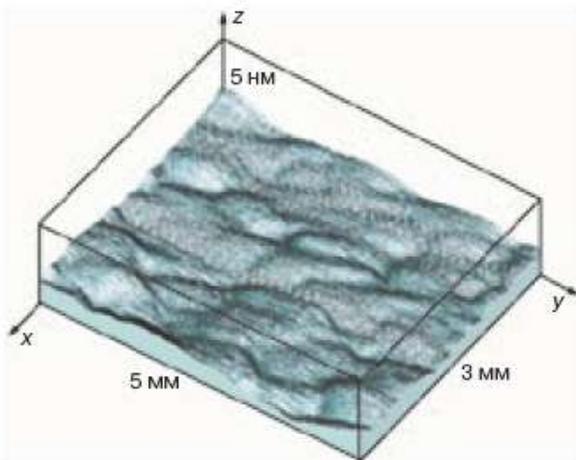


Reflectance for different thicknesses of metal films:  
 1) 10 nm, 2) 20 nm, 3) 30 nm, 4) 40 nm, 5) 50 nm  
 ( $\lambda=594$  nm)

Optical subwave microscope

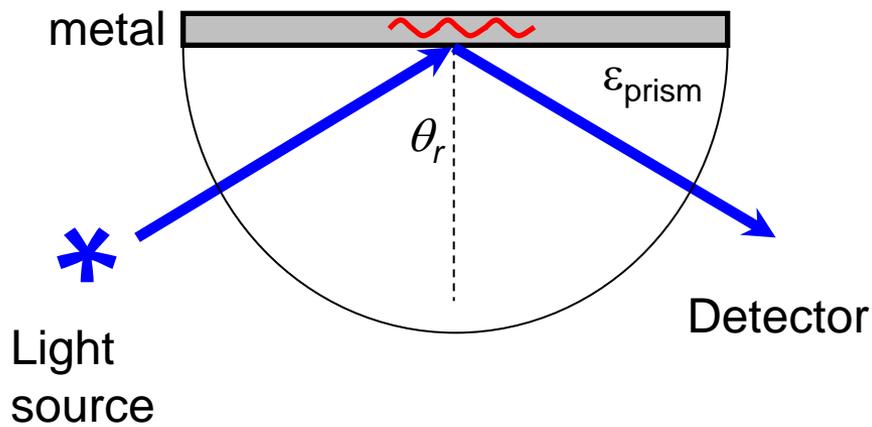


1 – laser, 2 – polarizer, 3 – presize stage,  
 4 – metallized prism, 5 – telescope, 6 –  
 photodetector

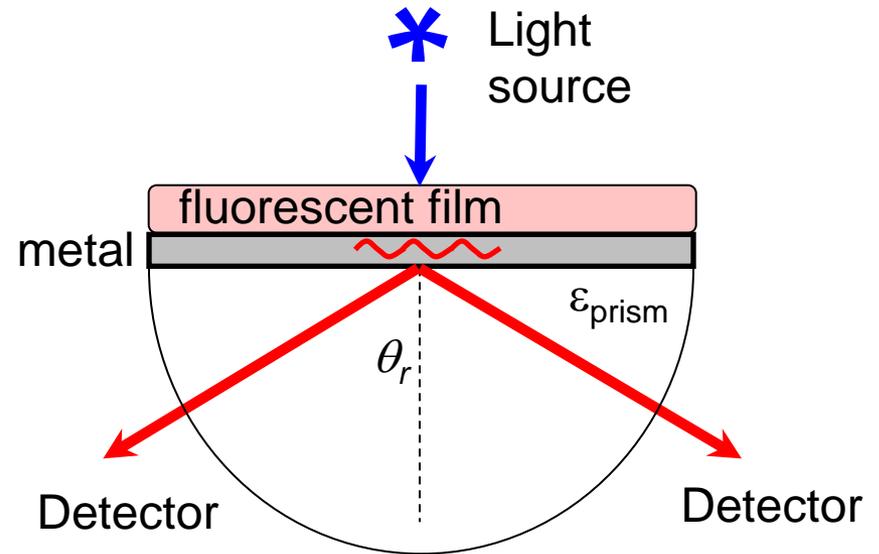


## 4. Modification of prism coupling scheme for the fluorescent materials.

## Kretschmann scheme



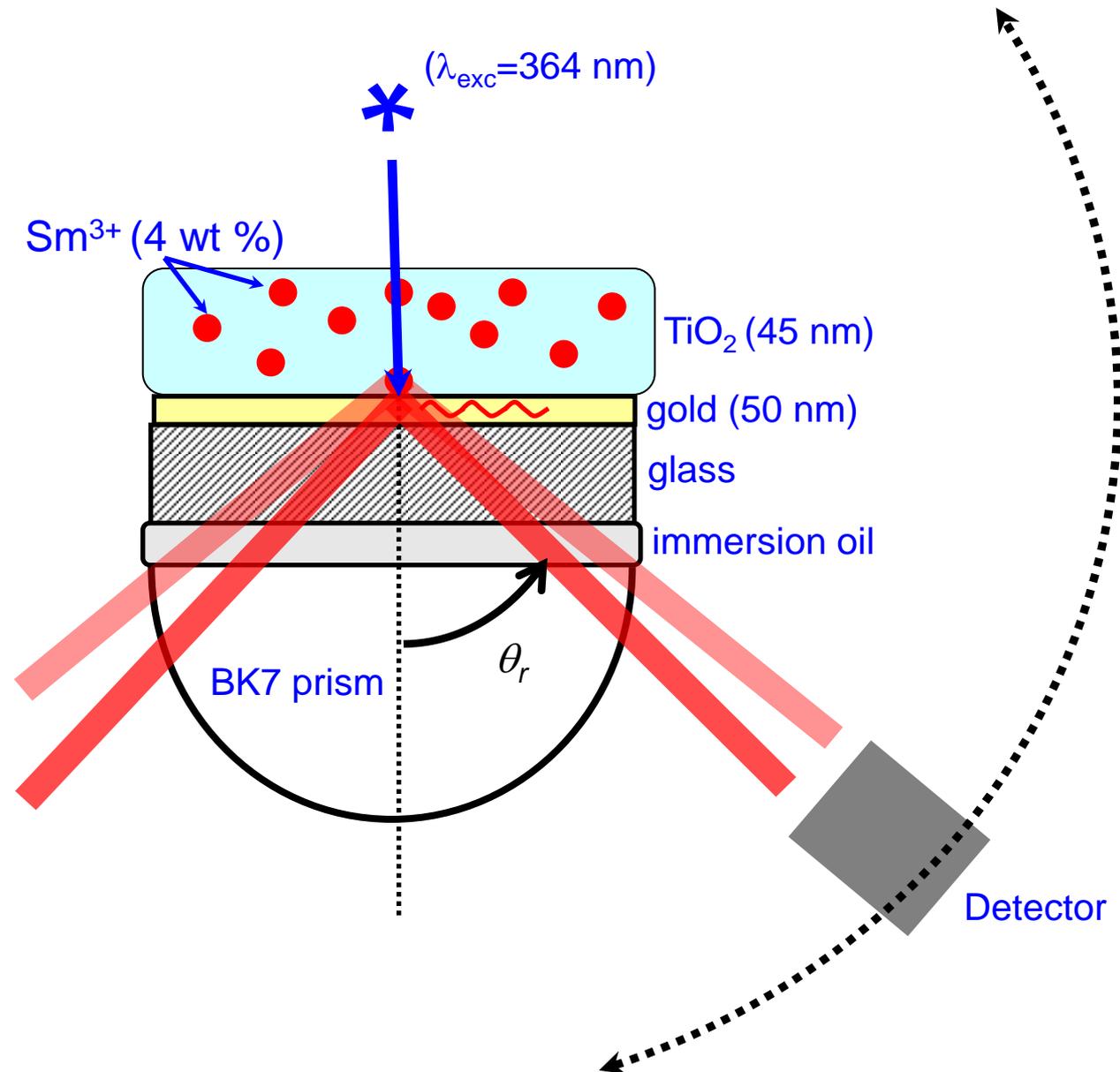
## Reverse Kretschmann scheme



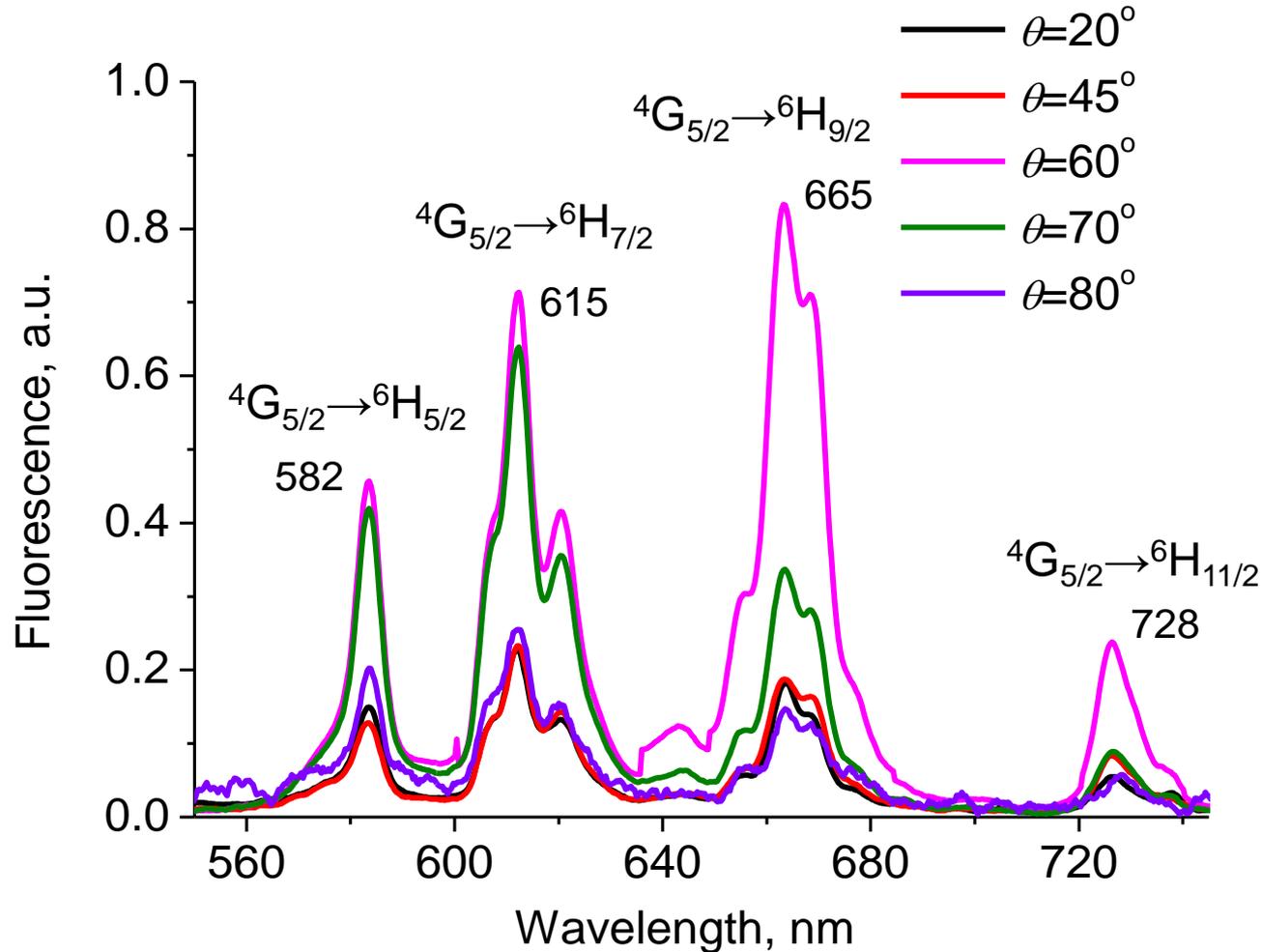
I. Gryczynski, J. Malicka, Z. Gryczynski, and J. R. Lakowicz // *Anal. Biochem.* Vol. 324, pp. 170-182, (2004).

Ray K. et al. / *Advances in Biochemical Engineering/Biotechnology*, Vol. 116 (2010).

# Reversed Kretschmann scheme for control $\text{Sm}^{3+}$ emission

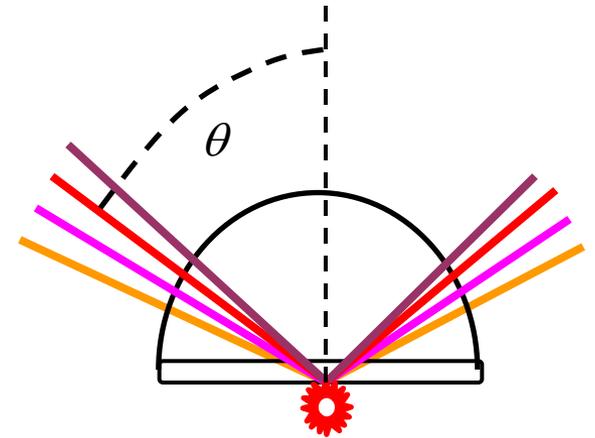
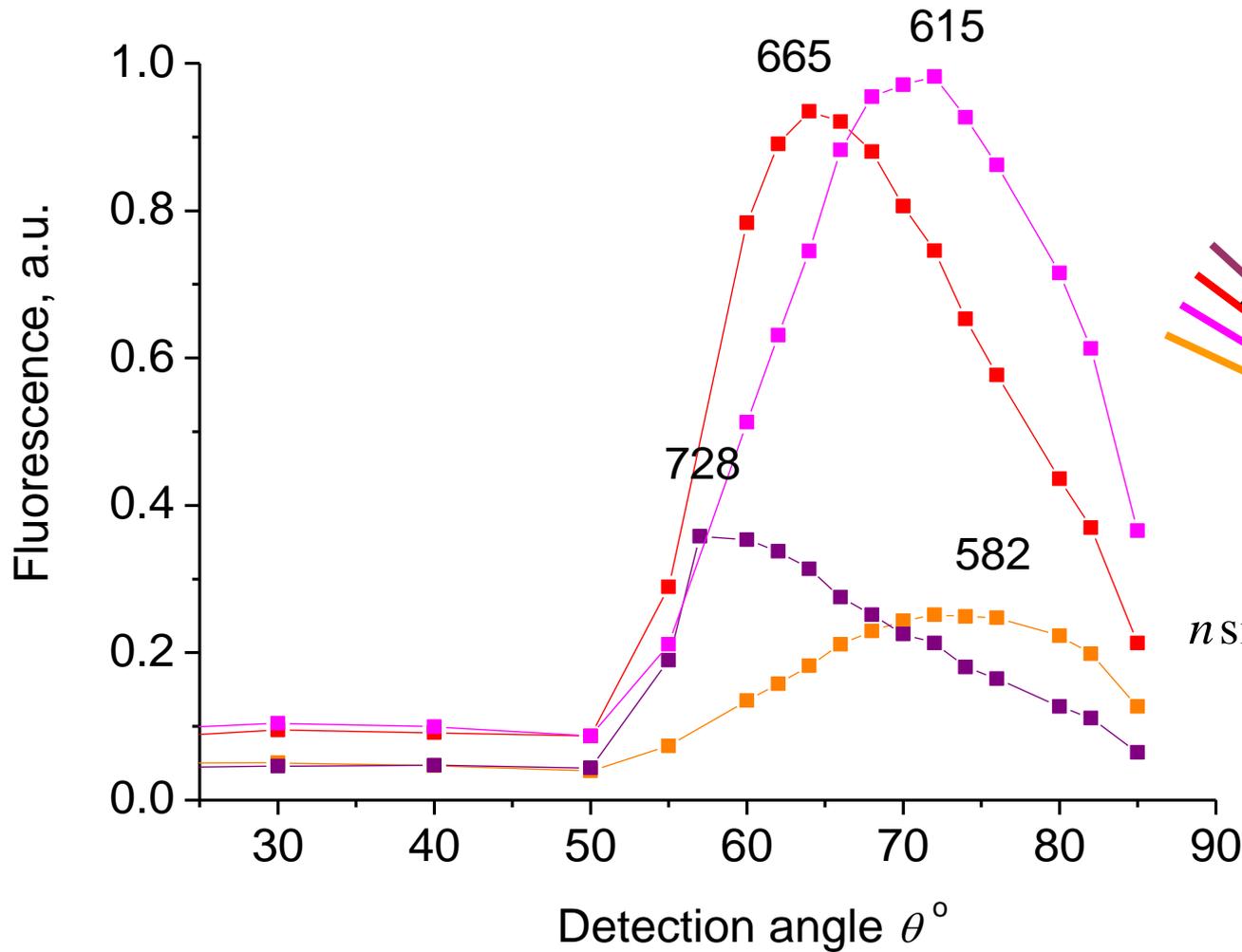


# Spectral distribution of fluorescent bands



Fluorescence of  $\text{Sm}^{3+}$  ions embedded into  $\text{TiO}_2$  films on the gold layer at different detection angles

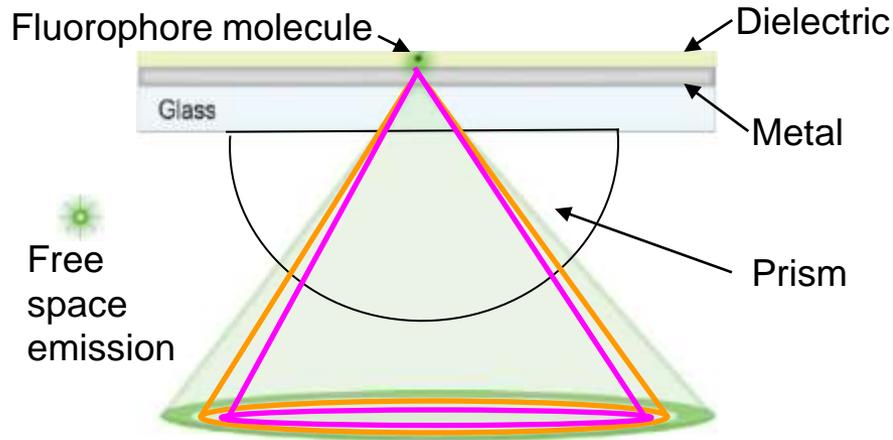
# Angular distribution of spectral bands



$$n \sin \theta_r = \sqrt{\frac{\epsilon_m'(\lambda) \cdot \epsilon(\lambda)}{\epsilon_m'(\lambda) + \epsilon(\lambda)}} + \beta$$

Angular dependences of intensity for spectral bands at 582, 615, 665 and 728 nm detected from  $\text{Sm}^{3+}$  ions embedded into  $\text{TiO}_2$  films on the gold layer

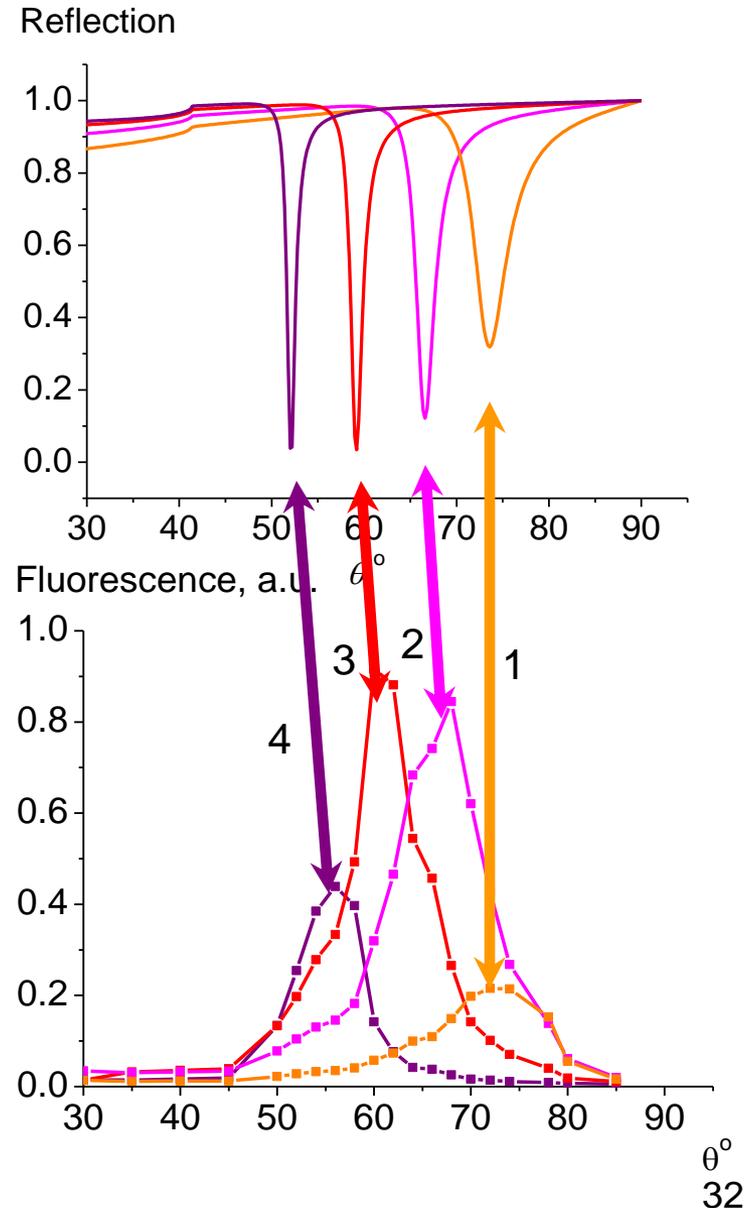
# Plasmon coupled directional emission



I. Gryczynski, J. Malicka, Z. Gryczynski, and J. R. Lakowicz // *Anal. Biochem.* Vol. 324, pp. 170-182, (2004).

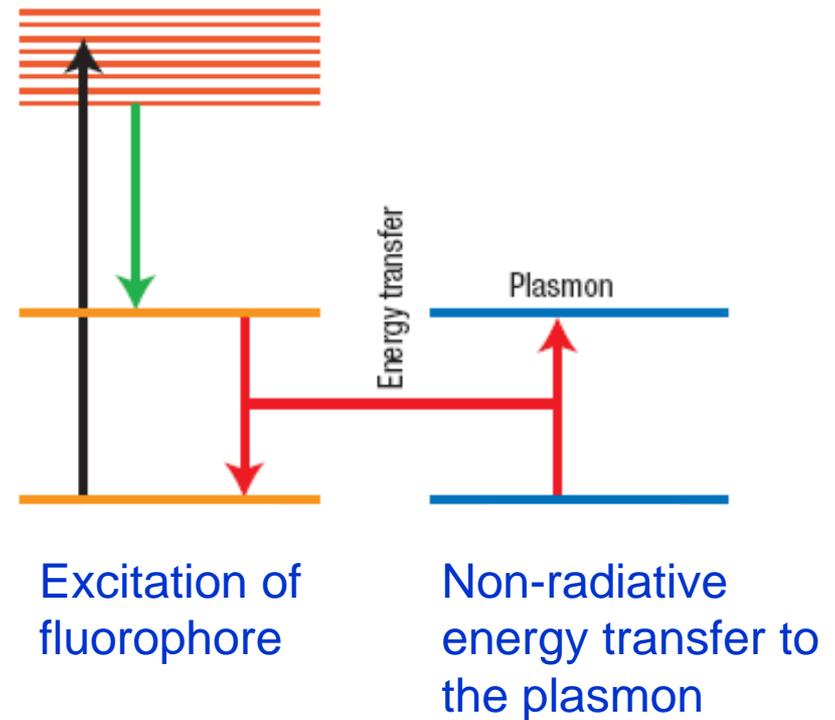
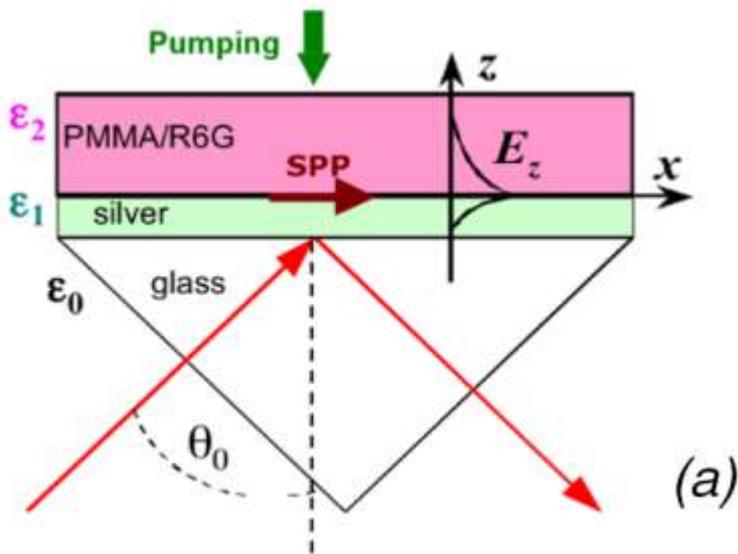
Correspondence between plasmonic dips and plasmon-coupled emission bands of  $\text{Sm}^{3+}$  ions in  $\text{TiO}_2$  film (100 nm) deposited on the gold layer (50 nm):

- 1) 583 nm,
- 2) 616 nm,
- 3) 665 nm,
- 4) 728 nm



Our data, Dolgov L. et al. // *Appl. Phys. B*, Vol. 107, pp. 749-753 (2012)

# Idea of SPASER: Surface Plasmon Amplification by Stimulated Emission of Radiation



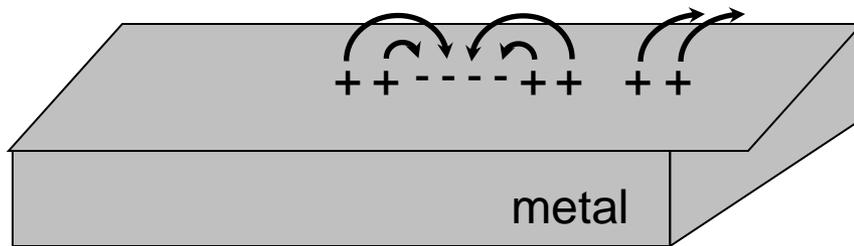
Stockman M. Spasers explained // Nature Photonics, Vol. 2, pp. 327-329 (2008)

Seidel J., Grafström S., and Eng L. // Phys. Rev. Lett. 94, 177401 (2005)

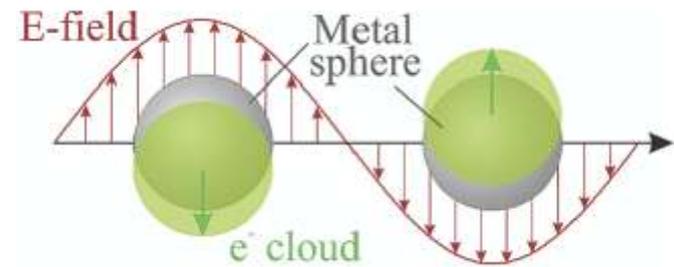
Noginov M. A. et al. // Phys. Rev. Lett., 101, 226806 (2008)

## 5. Some knowledge about localized plasmons

Plasmons propagating  
in metal layer

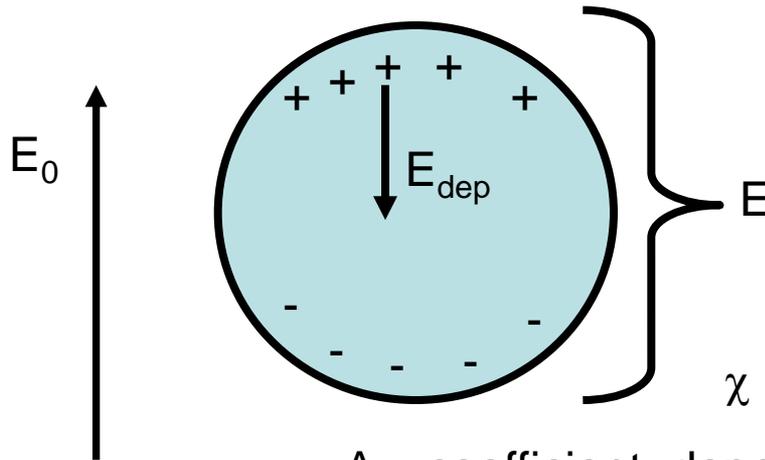


Plasmons localized in  
metal nanoparticles



Lakowicz J. R. Plasmonics in Biology and Plasmon-  
Controlled Fluorescence // Plasmonics Vol. 1, pp. 5-33  
(2006).

# Plasmonic resonance in nanoparticle: basic idea



$$E = E_0 - E_{\text{dep}}$$

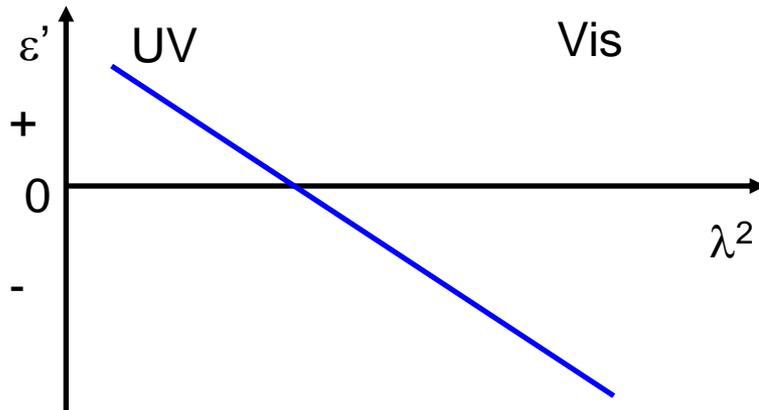
$$E_0 = E + E_{\text{dep}}$$

$$E_0 = E + \chi A E$$

$\chi$  - dielectrcital susceptibility,  $\chi = \varepsilon - 1$

A – coefficient, dependent on the geometry of the particle

*Wavelength dependence of  $\varepsilon'$  for noble metals*



$$E_0 = E + (\varepsilon - 1) A E$$

$$E_0 = E (1 + (\varepsilon - 1) A)$$

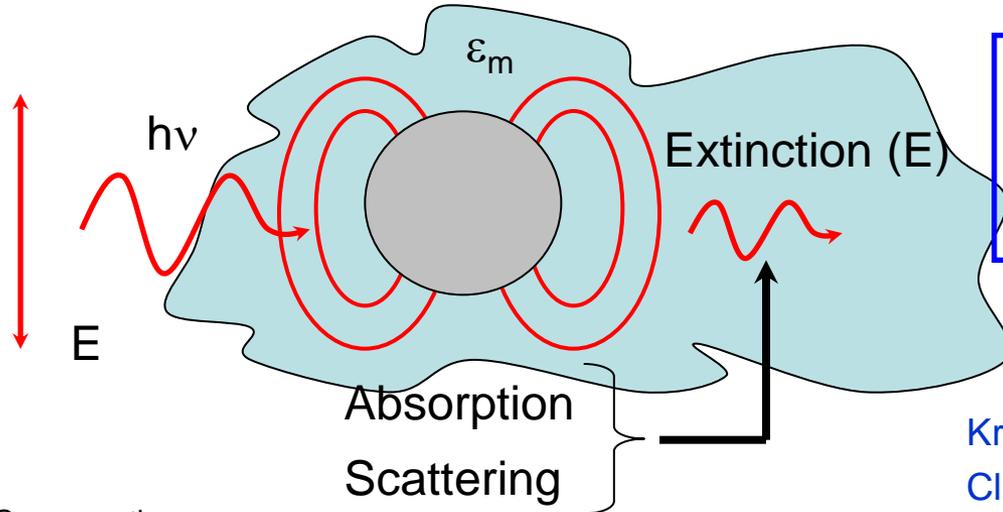
$$E = E_0 / (1 + (\varepsilon - 1) A)$$

for spherical particle  $A = 1/3$  and

$$E = 3E_0 / (2 + \varepsilon)$$

For metals at some frequencies  $\varepsilon \approx -2$  and **E increase increase strongly**

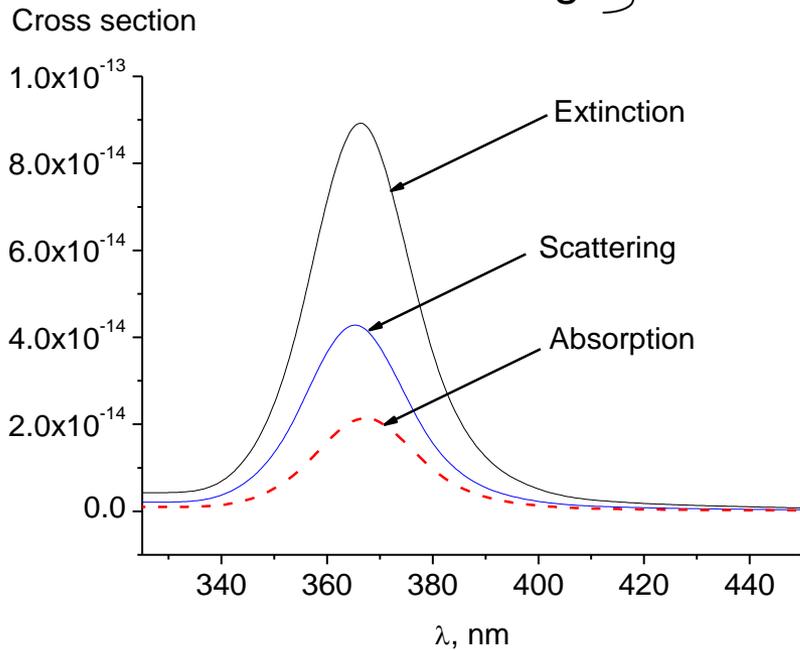
# Interaction of incident light with silver nanoparticle: plasmonic effect



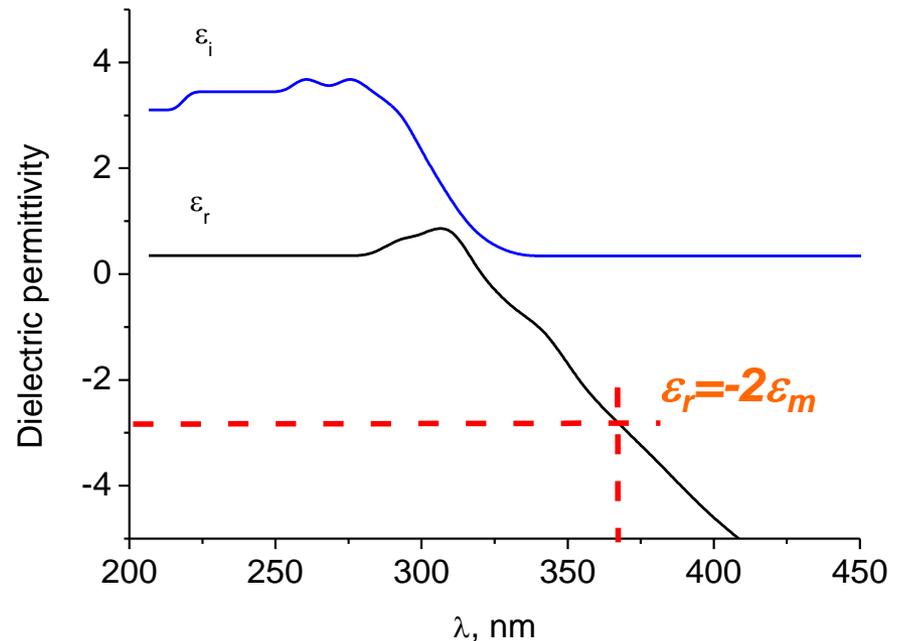
$$E = \frac{24\pi^2 N_A a^3 \epsilon_m^{3/2}}{\lambda \ln(10)} \left[ \frac{\epsilon_i}{(\epsilon_r + 2\epsilon_m)^2 + \epsilon_i^2} \right]$$

$\epsilon_r = -2\epsilon_m$  - resonance

Kreibig U., Vollmer M. Optical Properties of Metal Clusters. Springer-Verlag: Germany, 1995, Vol. 25.

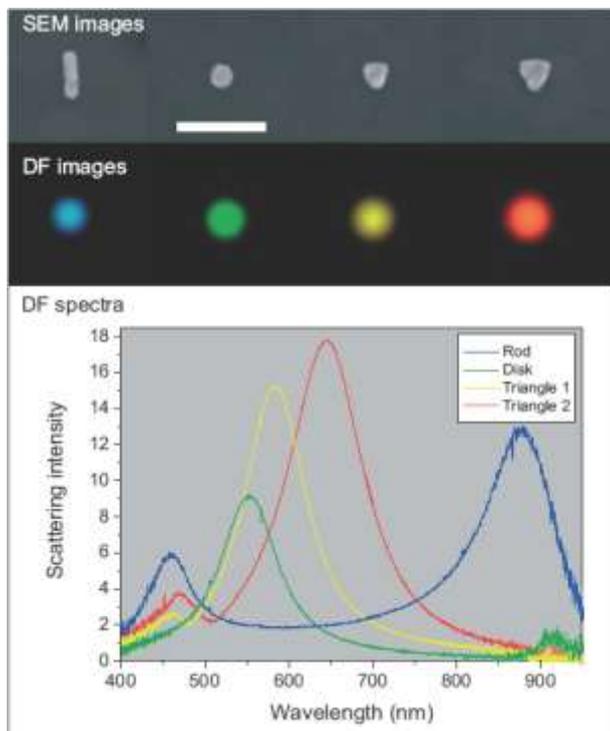


$a = 40 \text{ nm}, \epsilon_m = 1.35$



Silver dielectric permittivities 37

# How shape of nanoparticle can help in adjustment of spectral position of surface plasmon resonance



Relation between size, shape of nanoparticle and it's extinction spectra

Murray W.A., Barnes W.L. // Adv. Mater., V. 19, pp. 3771-3782, (2007).

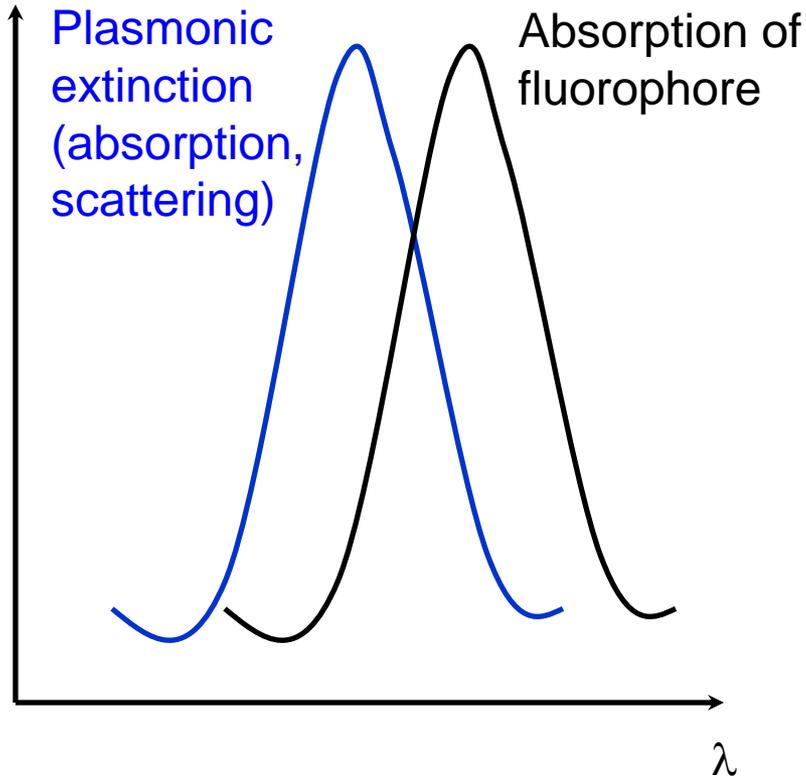
“Rainbow” from dispersions of silver nanoparticles



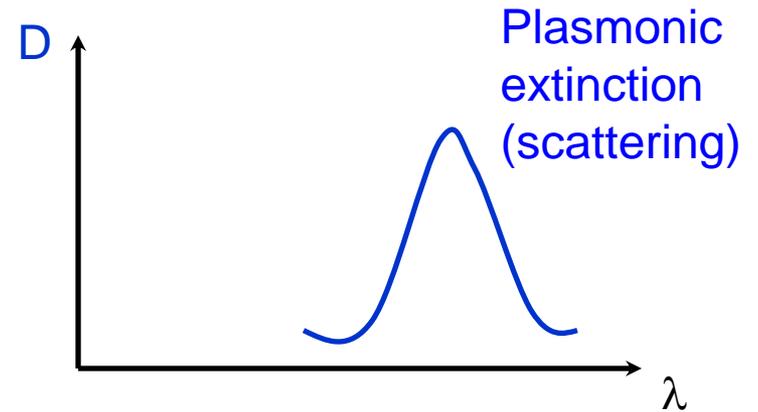
[http://www.nanometer.ru/2008/04/06/nanochastici\\_serebra\\_plazmon\\_cvet\\_11224.html](http://www.nanometer.ru/2008/04/06/nanochastici_serebra_plazmon_cvet_11224.html)

# Two ways for the enhancement of plasmon coupled fluorescence

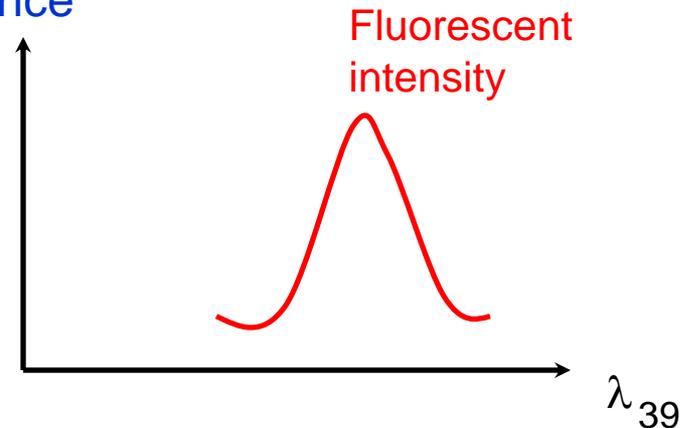
Plasmon resonance overlaps with fluorophore's light absorption D



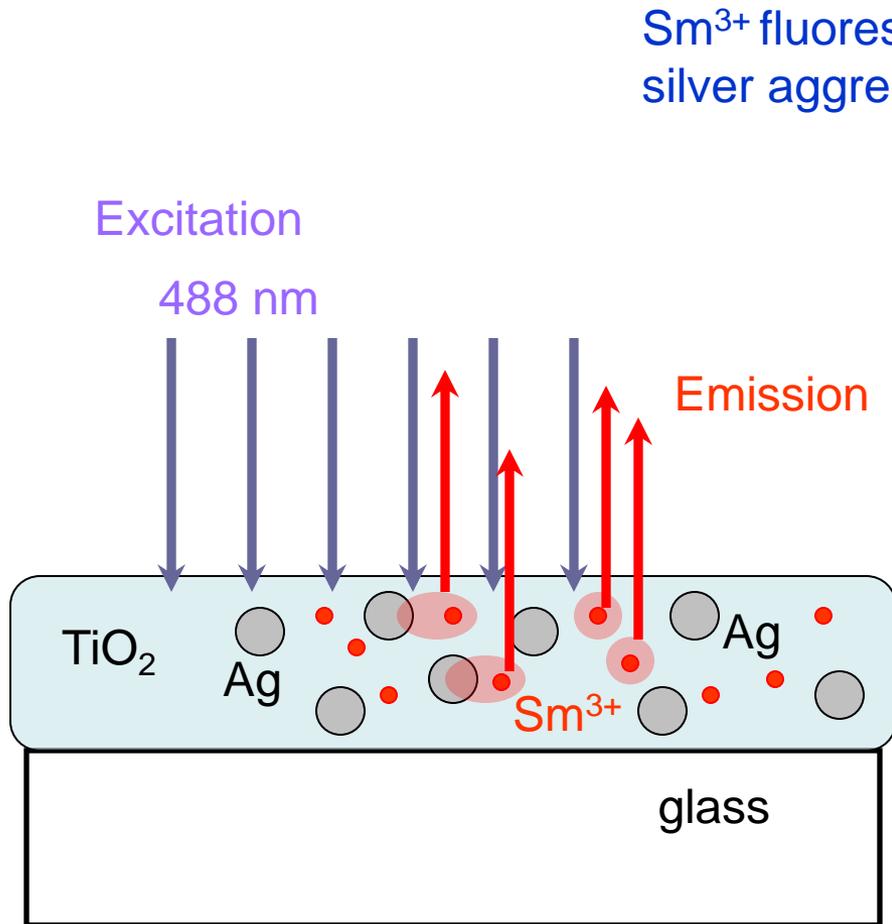
Plasmon resonance overlaps with fluorophore's light emission



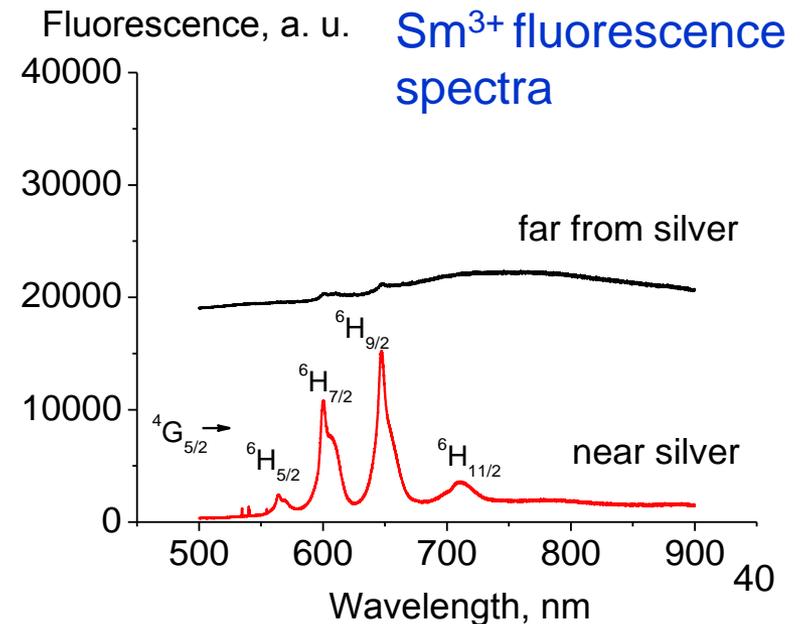
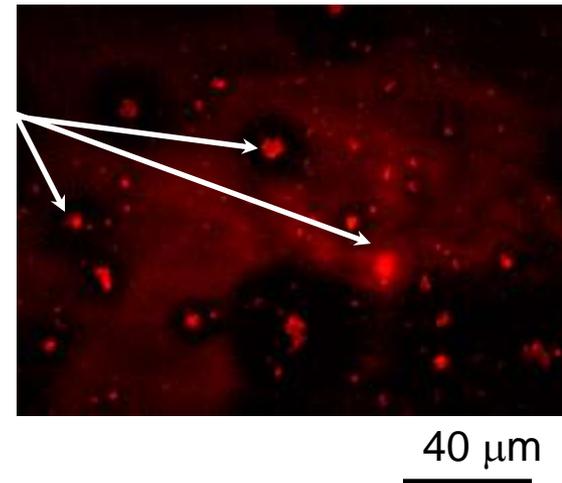
Fluorescence



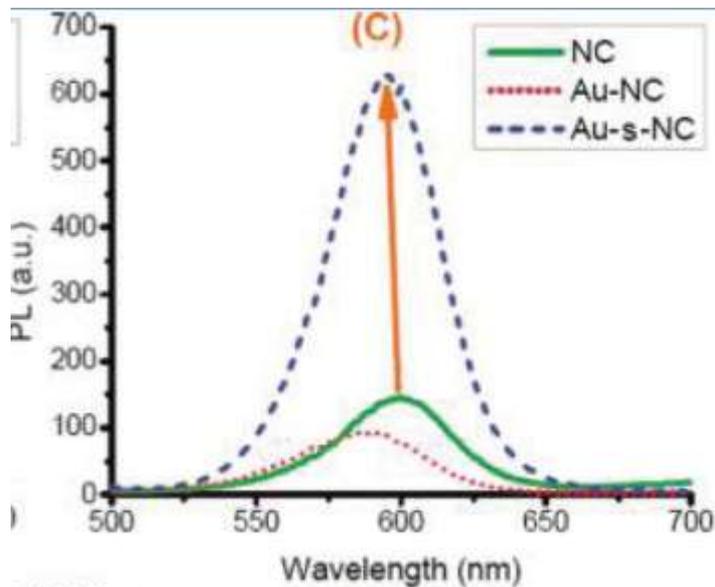
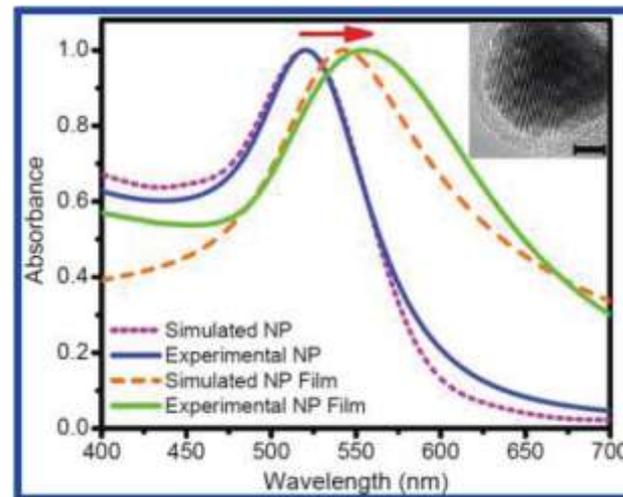
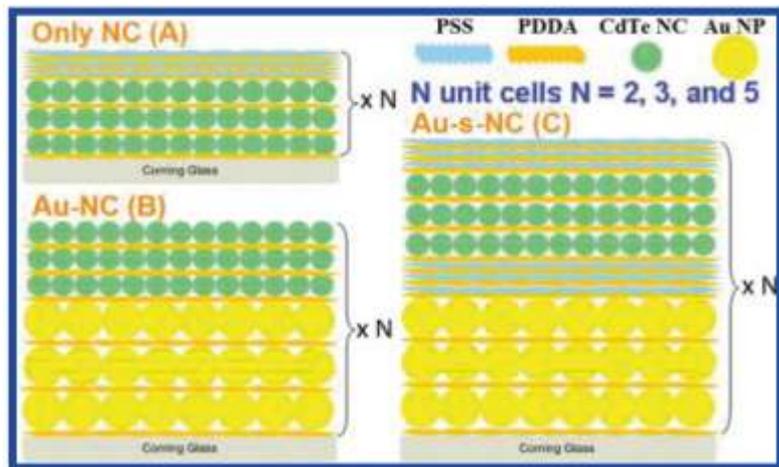
# Enhancement of $\text{Sm}^{3+}$ fluorescence by silver particles



$\text{Sm}^{3+}$  fluorescence near silver aggregate



# Enhancement of quantum dots fluorescence by gold particles



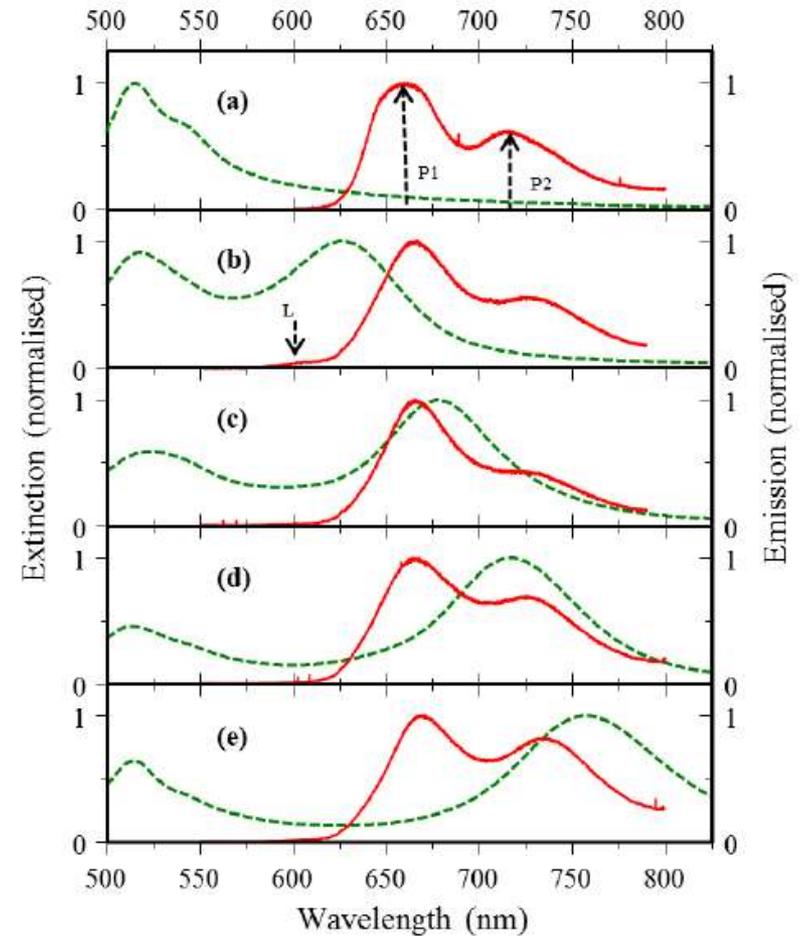
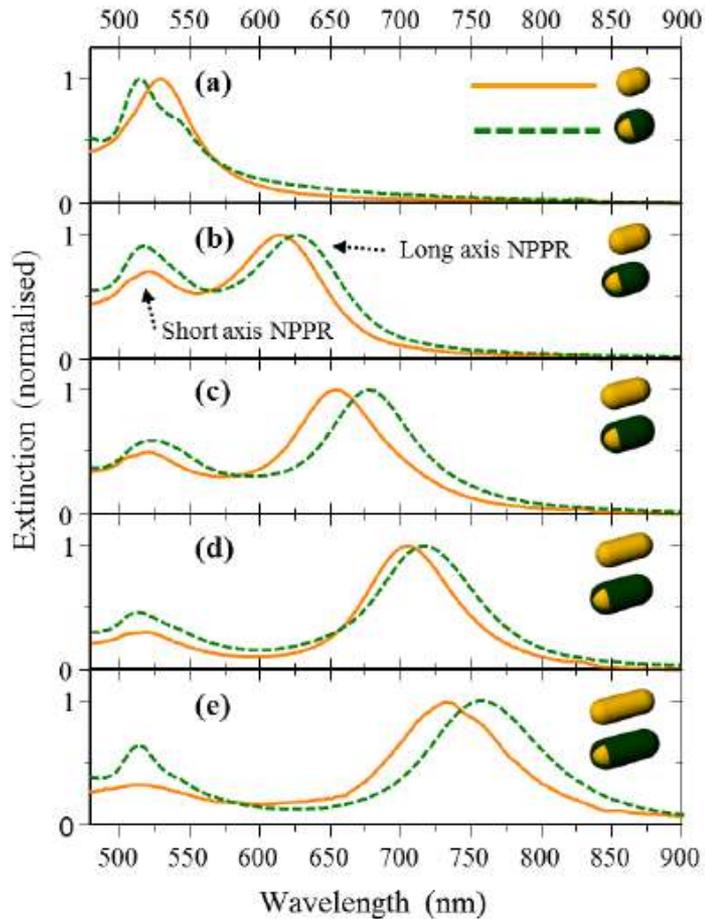
Photoluminescence of Cd-Te quantum dots placed on the gold nanoparticles (15 nm) layer-by-layer (5 layers):

NC – quantum dots without gold,

Au-NC – QDs with gold but without spacer layers

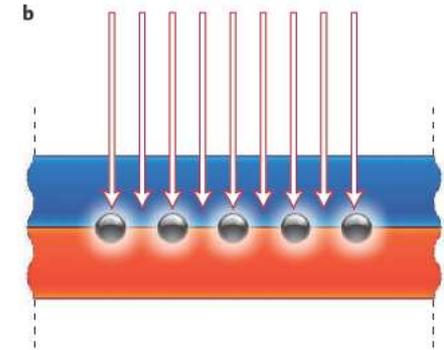
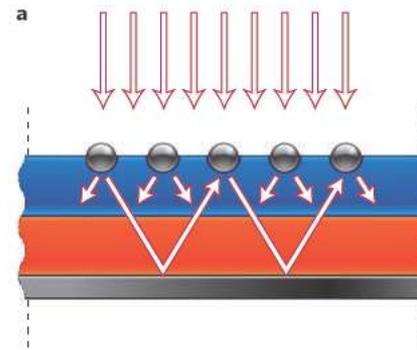
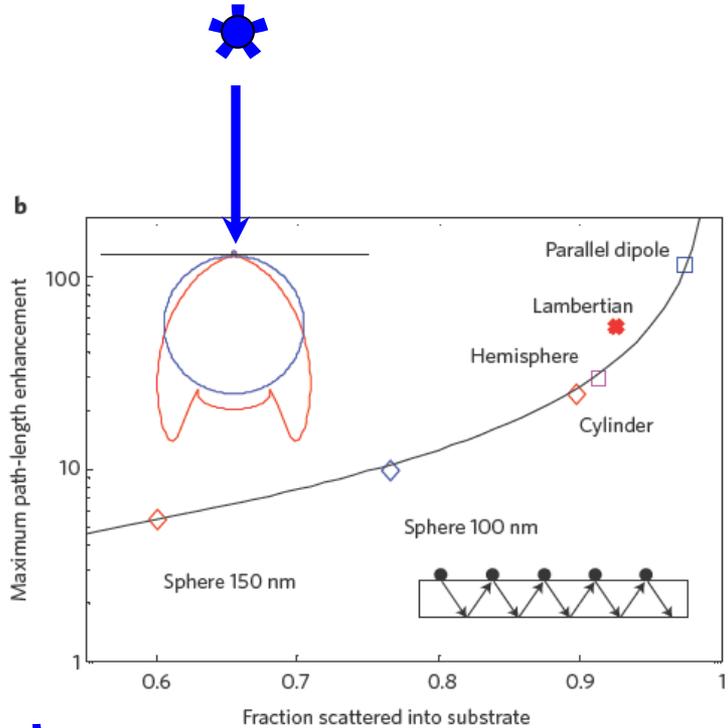
Au-NC - QDs with gold and spacer layers

# Enhancement of fluorescence by gold particles (example of porphyrin with several emission bands)



Djiango M., Ritter K., Müller R., Klar T. A. Spectral tuning of the phosphorescence from metalloporphyrins attached to gold nanorods // Optics Express, Vol. 20, No. 17 (2012).

# How plasmonic particle can enhance light trapping in solar cell



Nanoparticle as scatterer

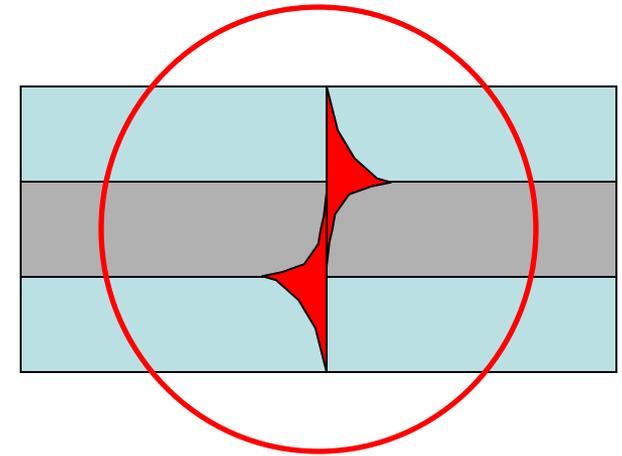
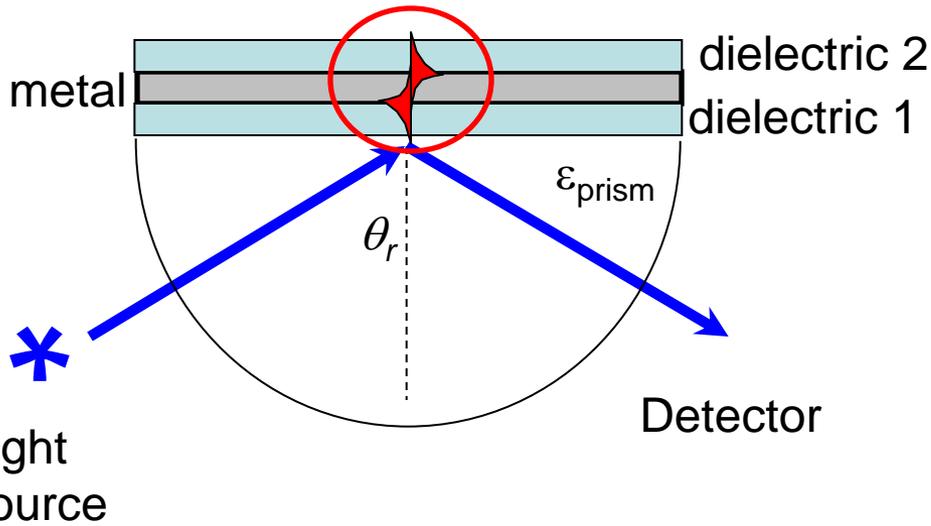
Nanoparticle as "antenna"

Atwater H. A., Polman A. Plasmonics for improved photovoltaic devices // Nature Materials, Vol. 9, pp. 205-213 (2010).

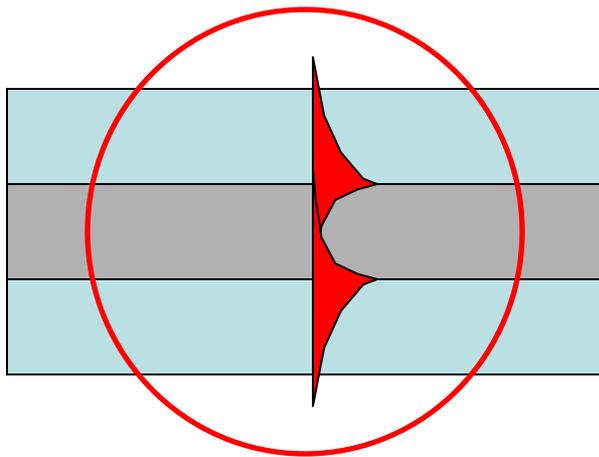
Different ways for excitation of plasmons.

# Other ways of excitation of surface plasmons and their application

## Otto scheme for inducing plasmons

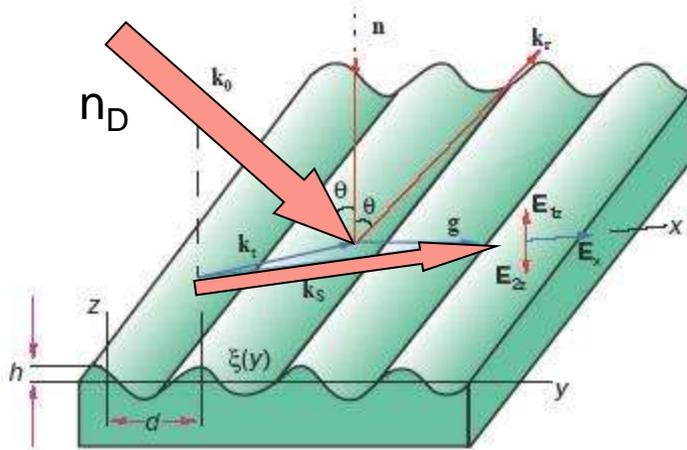


Antisymmetric distribution of the electric fields in the **short range plasmons**



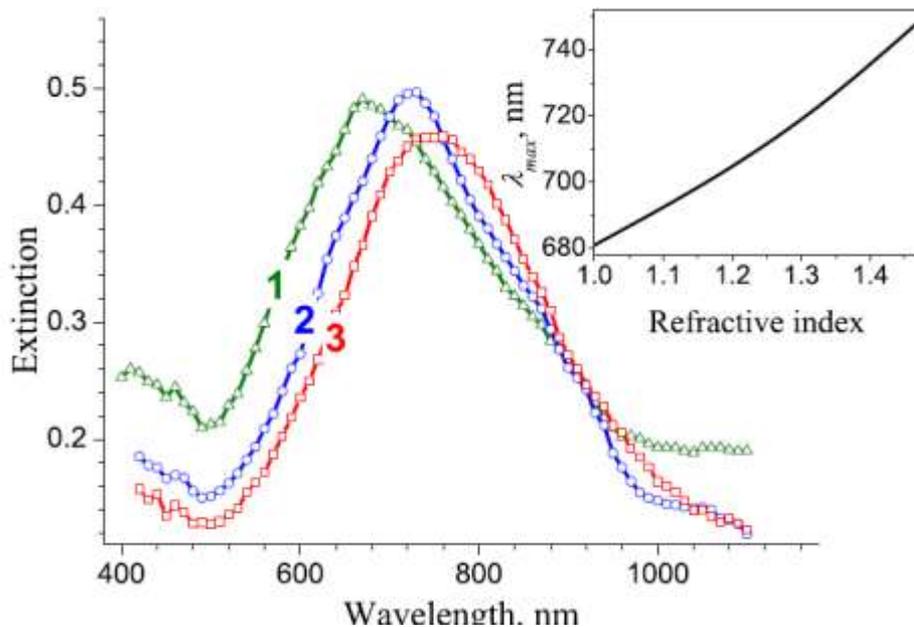
Symmetric distribution of the electric fields in the **long range plasmons**

# Inducing of surface plasmons on periodic metal gratings



$$n_D \sin \theta + m \frac{\lambda}{d} = \pm \sqrt{\frac{\epsilon_m n_D^2}{\epsilon_m + n_D^2}}$$

Libenson M. N // Soros Journal, No. 10, pp. 92-98 (1996).

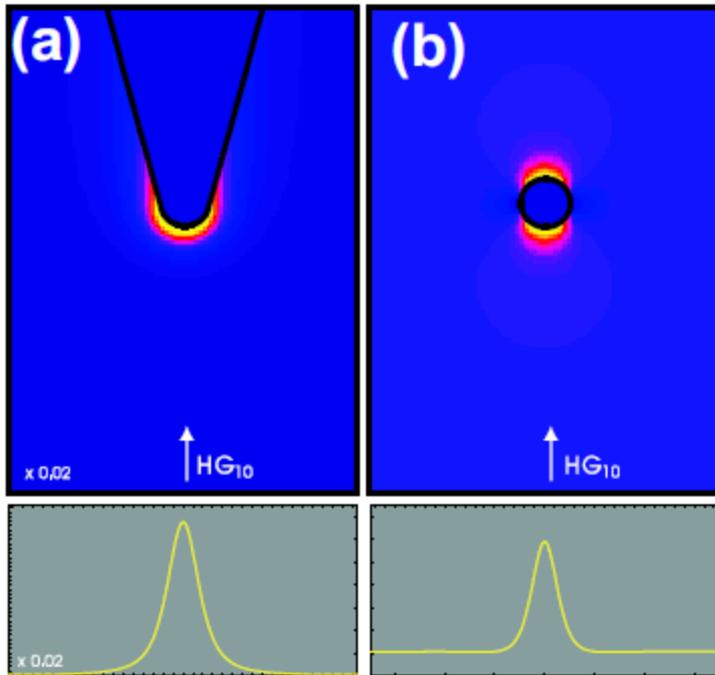


Sensitivity of the periodical array of golden nanowires deposited on the glass and immersed in different media:

1- air, 2- water, 3 - glycerine

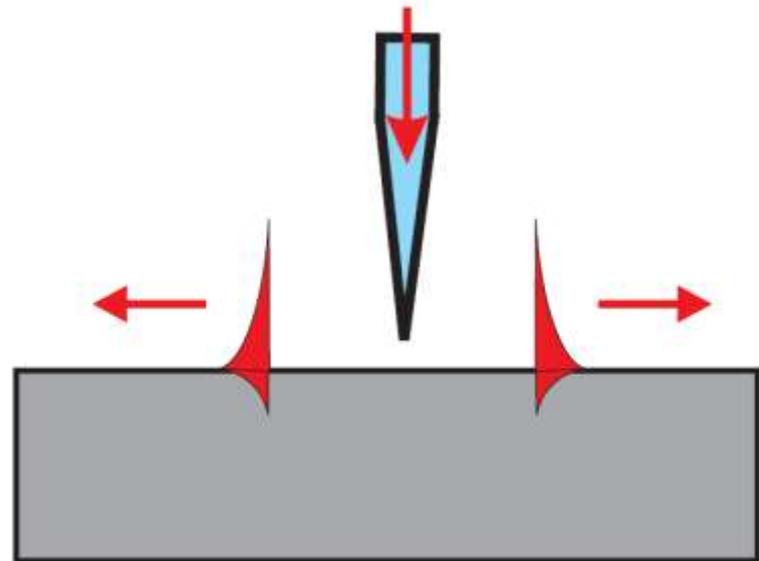
Sosnova et al. // Appl. Phys. B, Vol. 99, p. 493-497 (2010).

### Localization of electric field near metal tip and metal nanoparticle



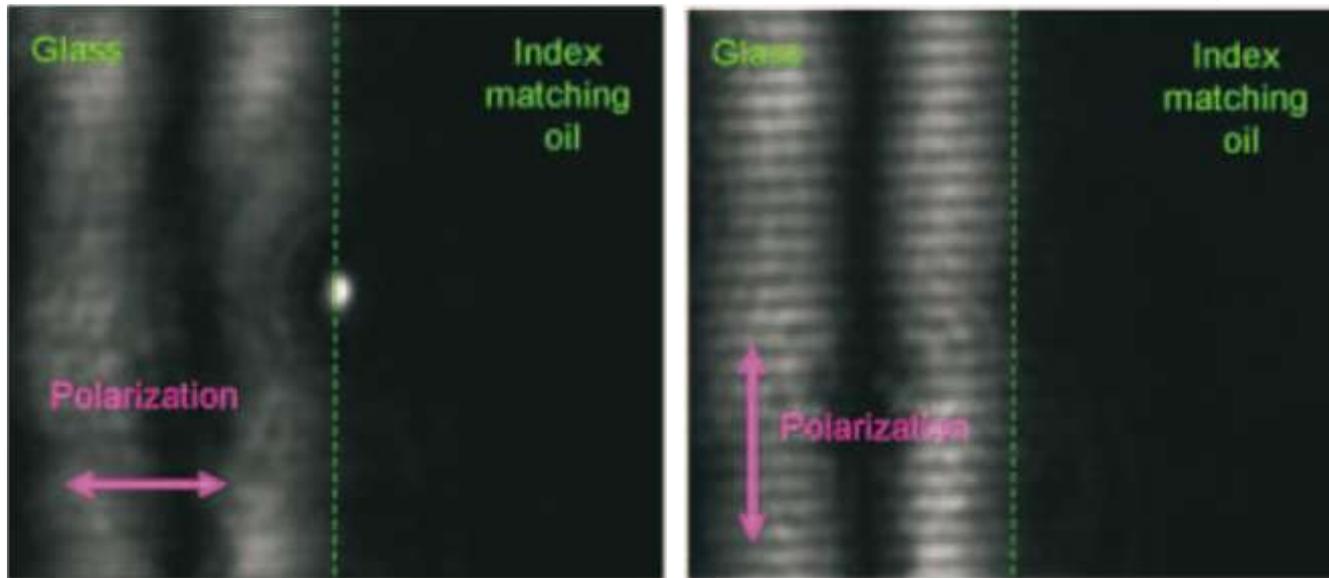
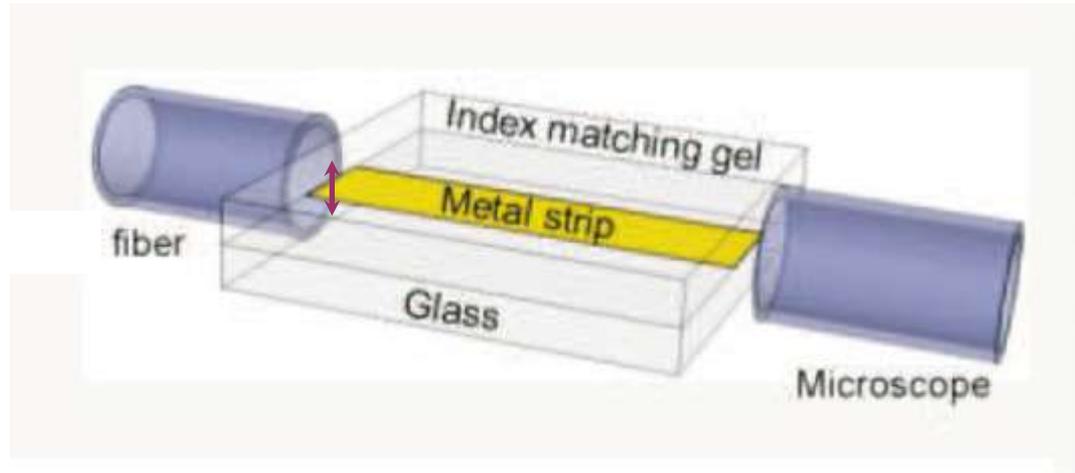
Surface Plasmon Nanophotonics. Series: Springer Series in Optical Sciences, Vol. 131 / Brongersma, Mark L.; Kik, Pieter G. (Eds.), 2007, VIII, 268 p.

### Near field excitation of surface plasmons



Zayats A.V. et.al. Nano-optics of surface plasmon polaritons // Physics Reports, Vol. 408, p. 131-314 (2005)

# Excitation of plasmon wave by end-fire coupling



# References

## For introduction

Sambles J. R., Bradbery G. W., Yang F. Optical excitation of surface plasmons: an introduction // Contemporary Physics, Vol. 32, No. 3, p. 173-183 (1991).

Handbook of Surface Plasmon Resonance / Edited by Richard B M Schasfoort and Anna J Tudos, RSC Publishing, 2008, Chapters 1, 2.

Surface Plasmon Resonance Based Sensors in Springer Series of Chemical Sensors and Biosensors, Vol 4., Editor J. Homola, 2006, Part 1.

V. M. Shalaev Metamaterials: A New Paradigm of Physics and Engineering. Internet course of lectures: <http://nanohub.org/resources/4262>

V. M. Shalaev Nanophotonics. Internet course of lectures: <http://nanohub.org/resources/1748>

# References

## For further reading

Raether H. Surface Plasmons on Smooth and Rough Surfaces and on Gratings.- Springer-Verlag, 1988.

Kreibig U., Vollmer M. Optical properties of Metal Clusters, Springer, 1995.

Maier S. A. Plasmonics: Fundamentals and Applications.- Springer, 2007.

## Sources in Russian Language

Поверхностные поляритоны, под ред. В. М. Аграновича, Д. Л. Миллса, М., 1985, перевод с английского

Майер С. А. Плазмоника: Теория и приложения. – Москва R&C Dynamics, 2011, перевод с английского.

Климов В. В. Наноплазмоника. – М., Физматлит, 2009.

Дмитрук Н. Л., Литовченко В. Г., Стрижевский В.Л. Поверхностные поляритоны в полупроводниках и диэлектриках. – Киев, Наукова думка, 1989.