

ABSTRACT

Structural parameters, elastic constants and thermodynamic properties of the tetragonal ternary Ag-based oxides LiAgO and NaAgO are investigated theoretically for the first time using the plane-wave ultra-soft pseudopotential method [1] based on the density functional theory [2,3]. The optimized lattice parameters and atomic positions agree well with the available theoretical and experimental counterparts. Pressure dependence of the structural parameters is also explored. Pressure dependences of the single-crystal elastic constants  $C_{ij}$  for LiAgO and NaAgO are explored. The elastic wave velocities propagating along the principal crystallographic directions are numerically estimated. The elastic anisotropy is estimated and further illustrated by 3D-direction-dependent of the Young's modulus. A set of some macroscopic elastic moduli, including the bulk, Young's and shear moduli, Poisson's coefficient, average elastic wave velocities and Debye temperature, were calculated for polycrystalline LiAgO and NaAgO from the  $C_{ij}$  via the Voigt-Reuss-Hill approximations [4–6]. Through the quasi-harmonic Debye model [7], which takes into account the phonon effects, the temperature and pressure dependencies of the bulk modulus, unit cell volume, volume thermal expansion coefficient, Debye temperature and volume constant and pressure constant heat capacities of LiAgO and NaAgO are explored systematically in the ranges of 0–20 GPa and 0–1200 K.

COMPUTATIONAL METHODS

The present calculations are carried out through the pseudopotential plane-wave method (PP-PW) as implemented in the CASTEP code [8]. The exchange-correlation interactions is treated by the PBEsol version of the generalized gradient approximation (the so-called GGA-PBEsol) [9]. An ultra-soft Vanderbilt-type pseudopotential is used to model the potential created by the nucleus and frozen electrons which applied to valence electrons. The Li:  $1s^2 2s^1$ , O:  $2s^2 2p^4$ , Ag:  $4d^{10} 5s^1$  and Na:  $2s^2 2p^6 3s^1$  electrons are treated as valence electrons. The plane-wave (PW) basis set, in which the electron wave functions are expanded, are truncated at a maximum plane-wave energy ( $E_{cut}$ ) of 400 eV. The Brillouin zone is sampled by Monkhorst–Pack special  $k$ -mesh.

The optimized structural parameters are reached through the Broyden-Fletcher-Goldfarb-Shanno (BFGS) minimization technique geometries [10]. The optimization convergence for energy change, maximal force, maximal stress and maximal displacement are fixed at  $5 \times 10^{-7}$  eV/atom, 0.01 eV/Å, 0.02 GPa and  $5.0 \times 10^{-4}$  Å, respectively. Gaussian scheme with a smearing width equal to 0.1 eV is used for the smearing of the electronic occupation. The finite strain-stress method is used to obtain the monocrystalline elastic constants ( $C_{ij}$ s) from which the polycrystalline elastic moduli are derived via the Voigt-Reuss-Hill approximation.

RESULTS

STRUCTURAL PROPERTIES

Table 1: Calculated equilibrium lattice parameters ( $a_0$  and  $c_0$ , in Å), internal coordinates ( $y_X$ ,  $x_{Ag}$  and  $x_O$ ), bulk modulus ( $B_0$ , in GPa), bulk modulus first pressure derivative ( $B'$ ) and bond lengths (Ag-O and X-O, in Å) for the ternary Ag-base oxides: LiAgO and NaAgO.

Parameter	Materials			
	LiAgO		NaAgO	
	Present	Expt.	Present	Expt.
$a$	9.176	9.248 <sup>c</sup>	9.429	9.522 <sup>c</sup>
$c$	3.816	3.75 <sup>c</sup>	4.655	4.602 <sup>c</sup>
$y_X$	0.415		4.699 <sup>b</sup>	4.599 <sup>d</sup>
			0.486 <sup>b</sup>	0.483 <sup>d</sup>
			0.49 <sup>e</sup>	
$x_{Ag}$	0.138		0.161	0.159 <sup>e</sup>
	0.162		0.158	0.306 <sup>e</sup>
$x_O$	0.322		0.310	
$B_0$	71.34		47.18	
			64 <sup>b</sup>	
$B'$	4.79		5.28	
$d_0(\text{Ag-O})$	2.0936		2.0737	
$d_0(\text{X-O})$	2.0663		2.3503	

<sup>b</sup> Ref. [11], <sup>c</sup> Ref. [12], <sup>d</sup> Ref. [13], <sup>e</sup> Ref. [14].

ELASTIC PROPERTIES

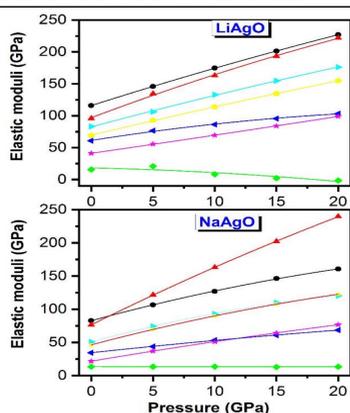


Fig. 1: Calculated pressure dependence of the elastic constants  $C_{ij}$  and bulk modulus  $B$  for the LiAgO and NaAgO materials. The symbols are the calculated results and the continuous lines are the second-order polynomial fits to the results

Table 2: Calculated elastic constants ( $C_{ij}$ , in GPa), Bulk modulus ( $B$ , in GPa), shear modulus ( $G$ , in GPa), Pugh's indicator ( $B/G$ ), Young's modulus ( $E$ , in GPa), Poisson's ratio ( $\sigma$ ), Lamé's coefficient ( $\lambda$ , in GPa), longitudinal, transverse and average sound velocities ( $V_l$ ,  $V_t$  and  $V_m$ , respectively, in m/s), and Debye temperature ( $\theta_D$ , in K) for the LiAgO and NaAgO materials.  $B$  is obtained from the  $C_{ij}$ s. The  $C_{ij}$ s of the isostructural compounds are given for comparison.

Parameter	Materials			
	LiAgO	LiCuO	NaAgO	NaCuO
$C_{11}$	116.1	125.5 <sup>a</sup>	82.9	86.4 <sup>a</sup>
$C_{33}$	95.976	94.3 <sup>a</sup>	76.4	73.8 <sup>a</sup>
$C_{44}$	15.8	25.1 <sup>a</sup>	13.6	15.4 <sup>a</sup>
$C_{66}$	60.9	58.7 <sup>a</sup>	34.6	34.7 <sup>a</sup>
$C_{12}$	83.3	72.7 <sup>a</sup>	51.0	41.8 <sup>a</sup>
$C_{13}$	41.1	40.0 <sup>a</sup>	21.7	21.3 <sup>a</sup>
$B_R$	69.4		46.5	
$B_V$	73.2		47.9	
$B_H$	71.3		47.2	
$G_R$	21.6		18.5	
$G_V$	29.3		22.2	
$G_H$	25.5		20.4	
$B_H/G_H$	2.8		2.32	
$E$	68.2		53.4	
$\sigma$	0.341		0.311	
$\lambda$	53.7		33.1	
$V_l$	4418.4		3970.9	
$V_t$	2172.6		2077.9	
$V_m$	2439.6		2324.4	
$\theta_D$	340.1		288.7	

THERMODYNAMIC PROPERTIES

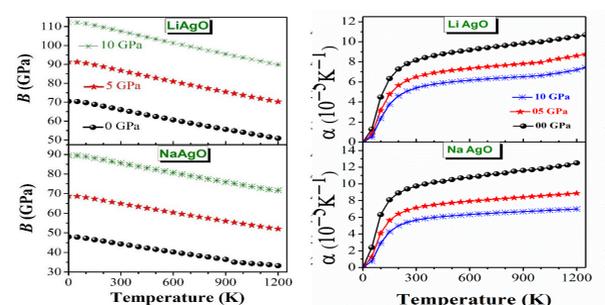


Fig. 2: Temperature dependence of the bulk modulus and the volume thermal expansion coefficient under the various pressures for LiAgO and NaAgO.

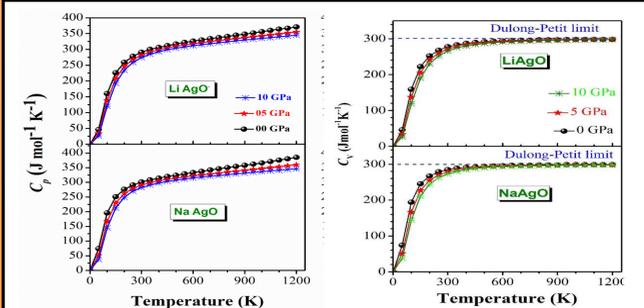


Fig. 3. Temperature dependence of the constant pressure heat capacity and the constant volume heat capacity under the various pressures for LiAgO and NaAgO.

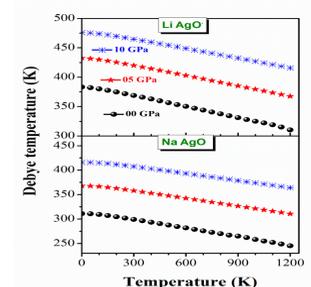


Fig. 4. Temperature dependence of the Debye temperature under the various pressures for LiAgO and NaAgO.

CONCLUSION

- ✓ *Ab initio* calculations of the structural, elastic and thermodynamic properties for the Ag-based oxides  $X\text{AgO}$  ( $X = \text{Li}$  and  $\text{Na}$ ) have been performed in the present work.
- ✓ Good agreement is found between the optimized lattice parameters and the existing experimental values. An anisotropic behavior of the pressure dependence of the lattice constants is also found.
- ✓ All studied materials are mechanically stable at zero pressure with a strong elastic anisotropy.
- ✓ According to Pugh's criterion, all studied materials behave in a brittle manner.
- ✓ The temperature and pressure dependencies of the bulk modulus, unit cell volume, heat capacity, volume thermal expansion coefficient and Debye temperature are also studied in 0–1200 K and 0–20 GPa ranges via the quasi-harmonic Debye model.

REFERENCES

1. Vanderbilt D. Soft self-consistent pseudopotentials in a generalized eigenvalue formalism // Phys. Rev. B -1990.- 41.- P. 7892-7895.
2. Hohenberg P., Kohn W. Phys. Rev. B-1964.-136.- P. 684.
3. Kohn W., Sham L.J. Phys. Rev. A-1965.-140.- P. 1133.
4. Reuss A. Zeitschrift für Angewandte Mathematik und Mechanik-1929.-9.- P. 49-58.
5. Hill R. Proc. Phys. Soc. A-1952.-65.- P. 349-354.
6. Hill R. elastic properties of reinforced solids : some theoretical principles // J. Mech. Phys. Solids-1963.-11.- P. 357-372.
7. Blanco M.A., Francisco E., Luaña V., GIBBS. isothermal-isobaric thermodynamics of solids from energy curves using a quasi-harmonic Debye model // Comput. Phys. Commun.-2004.-158.- P. 57-72.